

1 Asymmetric dynamical behavior of thermochemical 2 plumes and implications for Hawaiian lava 3 composition

4 Maxim D. Ballmer*¹, Garrett Ito¹, and Cheng Cheng²

5 (1) School of Ocean and Earth Sciences and Technology, University of Hawaii at Manoa, 1680 East-West
6 Road, Honolulu, HI 96822, USA. (2) Dept. Earth and Planetary Sciences, University of California, 307
7 McCone Hall, Berkeley, CA 94720, USA. (*) corresponding author: ballmer@hawaii.edu

8

9 Abstract

10 The Hawaiian Kea and Loa volcano trends have commonly been interpreted as directly
11 reflecting a compositional zonation within the Hawaiian plume stem, inherited from the
12 lowermost mantle. As this zonation is often associated with variations in mafic material, and as
13 such materials, especially eclogites, impact mantle flow, this study aims to characterize the
14 ascent and melting of bilaterally-zoned thermochemical plumes. Our geodynamic models predict
15 that plumes bearing $\gtrsim 12\%$ eclogite tend to stagnate as a deep eclogitic pool (DEP) in the mid-
16 upper mantle where phase changes lead to a maximum in eclogite excess density. This behavior
17 can explain recent seismic-tomography results, and predicts thermal asymmetry of material
18 rising out of the DEP to feed the hotspot. Thermal asymmetry is caused by the effects of
19 ambient-mantle flow or plume-stem zonation on DEP dynamics, and ultimately boosts peridotite
20 melting on the melting zone's hotter side. This hotter side is hence less dominated by melting of
21 mafic materials, despite being fed by equally or *more* such materials than the cooler side. These
22 results suggest that the Kea side of the Hawaiian Plume is equally or more eclogitic than the Loa
23 side, opposite to previous interpretations. Care should thus be taken in mapping geographical
24 variations in lava chemistry into the deep mantle.

25

26 1. Introduction

27 Better constraints on the make-up of the deep mantle are needed to advance our
28 understanding of the differentiation and secular evolution of our planet (cf. Boyet and Carlson,
29 2005; Labrosse et al., 2007). In the framework of mantle plume theory, hotspot lavas provide one
30 of the most important means of probing the composition of the deep mantle. For example, the
31 global-scale DUPAL anomaly among hotspot lavas (Dupre and Allegre, 1983) has been
32 associated with the seismically imaged large low shear-wave velocity provinces (LLSVPs)
33 (Castillo et al., 1998; Wen et al., 2001; Wen, 2006). These LLSVPs are compositionally dense

34 structures in the deep mantle (Ishii and Tromp, 1999; Masters et al., 2000; Mosca et al., 2012),
35 from the margins of which most mantle plumes are inferred to rise (Burke and Torsvik, 2004;
36 2006; Torsvik et al., 2010). Regional geographical variations in ocean-island basalt geochemistry
37 have also been interpreted as reflecting lower-mantle compositional heterogeneity in the Pacific
38 (e.g., Konter et al., 2008).

39 Similarly, local-scale geographical variations of lava geochemistry within single hotspot
40 chains, such as within the Marquesas, Society and Samoa chains, are interpreted as reflecting
41 heterogeneity in the deep mantle (Workman et al., 2004; Huang et al., 2011; Chauvel et al.,
42 2012; Payne et al., 2013). Another example that has recently attracted a great deal of interest is
43 the bilateral geochemical asymmetry of Hawaiian volcanism (Fig. 1). The Hawaiian Islands have
44 long been interpreted to be a double chain of volcanoes (Jackson et al., 1972), of which the
45 prevalent morphological trends, the southwestern “Loa” and the northeastern “Kea” trend,
46 display distinct geochemical signatures (Frey and Rhodes, 1993; Kurz et al., 1996; Abouchami et
47 al., 2005; Weis et al., 2011). This distinction has been interpreted as revealing a bilateral
48 compositional zonation of the deep plume conduit (e.g., Abouchami et al., 2005). *Huang et al.*
49 (2011) and *Weis et al.* (2011) argue that the Hawaiian Plume—as apparently rising from the
50 margin of a LLSVP—entrains compositionally distinct materials into either sides of the plume
51 stem.

52 The possibility that entrainment of distinct materials may be expressed in hotspot-lava
53 composition requires that plumes rise with little lateral material exchange or rotation across their
54 conduits (about a vertical axis). In classical theory, plumes are described as upwellings that rise
55 near-vertically through the entire mantle to support magmatism, purely driven by thermal
56 buoyancy (Morgan, 1972; Griffiths and Campbell, 1990; Sleep, 1990; Ribe and Christensen,
57 1994). Based on such purely thermal plume models (i.e., with density being independent of
58 composition), *Farnetani and Hofmann* (2009; 2010) demonstrate that patterns of deep-mantle
59 composition can indeed be directly reflected by geographic variations in hotspot-lava
60 geochemistry. However, the Hawaiian Plume is thought to carry compositionally dense, mafic
61 materials (e.g., entrained from the LLSVP or a slab graveyard), thereby potentially behaving
62 more complexly than a classical plume (e.g., Farnetani and Samuel, 2005), particularly if these
63 materials are initially distributed non-uniformly, or even bilaterally asymmetrically, within the
64 deep part of the plume stem.

65 Evidence for the presence of mafic materials (e.g., pyroxenite or eclogite) in the source of
66 Hawaiian lavas comes from major-element, trace-element, as well as isotopic data (Hauri, 1996;
67 Huang and Frey, 2005; Sobolev et al., 2005, 2007; Huang et al., 2007; Herzberg, 2011; Jackson
68 et al., 2012; Pietruszka et al., 2013). These materials are inferred to be more abundant in the
69 source of Loa, than of Kea volcanoes, and are likely to contribute to the geochemical distinction
70 between the two trends (Sobolev et al., 2005; Greene et al., 2010; Jackson et al., 2012).

71 Eclogites are significantly denser than peridotites and thus strongly affect plume ascent.
72 Analogue and numerical geodynamic models show that such eclogitic or “thermochemical”
73 plumes display asymmetric and time-dependent behavior (Davaille, 1999; Farnetani and Samuel,
74 2005; Lin and van Keken, 2005; Kumagai et al., 2008), much in contrast to classical-plume
75 behavior—which so far has inspired the interpretations of geochemical asymmetry of Hawaiian
76 lavas. This complex behavior is caused by the competition between diffusive, positive thermal
77 buoyancy and non-diffusive, negative compositional buoyancy in thermochemical plumes. Phase
78 transitions can account for additional complications (e.g., Farnetani and Samuel, 2005). For
79 example, *Ballmer et al.* (2013) show that a peak in the excess density of eclogite relative to
80 peridotite due to phase changes in the olivine and quartz systems (Aoki and Takahashi, 2004)
81 can cause thermochemical (i.e., eclogitic) plumes to pool in a broad layer at 300~410 km depth
82 (“deep eclogitic pool”, DEP) before rising to feed the hotspot (Fig. 2).

83 Evidence for such complex dynamical behavior beneath the Hawaiian hotspot is provided by
84 recent seismic tomography. Body-wave tomography, based on data collected during the regional
85 Plume and Lithosphere Undersea Melt Experiment (PLUME), images a thick (~400 km),
86 asymmetric body of slow seismic velocities beneath the hotspot (Wolfe et al., 2009, 2011). These
87 seismic models disagree with classical plume theory, which predicts a much thinner (<100 km)
88 and symmetric layer (“pancake”) to pond beneath the lithosphere. The presence of a large
89 volumes of low-velocity materials is further supported by a recent joint inversion of body waves,
90 surface waves, and ambient noise recorded by PLUME (Cheng et al., this volume). In addition to
91 body-wave tomography alone, these joint inversions resolve two layers of seismically slow
92 material in the upper mantle: one beneath the lithosphere (at ~100 km depth), and another one
93 contained in the depth range of ~250 km to ~450 km (Fig. 3; Cheng et al.’s (this volume)).
94 Seismic resolution tests indicate that these seismic constraints are consistent with the presence of
95 a double-layered (DEP and pancake) thermochemical plume beneath Hawaiian hotspot (Ballmer
96 et al., 2013; Cheng et al., this volume).

97 In this study, we explore the dynamics of bilaterally asymmetric thermochemical plumes in
98 which one side of the plume carries a higher fraction of compositionally dense materials (such as
99 eclogite) than the other side. By predicting geographical patterns of volcanism due to the melting
100 of mafic and ultramafic source lithologies, we investigate the link between the deep
101 compositional zonation and geographical variations in lava composition. Our results show that
102 thermochemical plume dynamics in the upper mantle can create geographical patterns of lava
103 composition independent of a zonation in the deep plume conduit. They can veil, or even
104 apparently reverse, any deep bilateral zonation.

105

106 **2. Methods and model description**

107 We use a Cartesian version of the finite-element code Citcom (Moresi et al., 1996) to model
 108 thermochemical-plume dynamics. The model domain of length 5280 km (x -direction), width
 109 3300 km (y -direction), and height 660 km (z -direction) is discretized in $768 \times 512 \times 96$ finite
 110 elements with the smallest elements (i.e., $4.5 \times 4.5 \times 4.5$ km) located in the asthenosphere near
 111 the hotspot. This fine resolution is needed to accurately model melting processes and predict
 112 magma compositions. A horizontal velocity in the x -direction of $v_{plate} = 80$ km/Myr is imposed at
 113 the top boundary to simulate Pacific plate motion. All boundaries, except for the front ($x = 0$) and
 114 back sides ($x = 5280$ km) are closed to in- and outflow. At a distance of 3135 km from the front
 115 side (i.e., inflow boundary), 2145 km from the back side (i.e., outflow boundary), and 1650 km
 116 from both lateral side boundaries, a Gaussian thermal anomaly of half-width r_P (see Table 1) and
 117 amplitude of +300 K is imposed to supply a plume at the base of the model. Upward flow of
 118 plume material into the model domain (i.e., from the lower, into the upper mantle) is only
 119 allowed within a radius of $4.8r_P$ from the plume center, where the bottom boundary is locally
 120 open to vertical flow.

121 In the core of the plume, a cylinder of radius r_E is taken to contain eclogite (Fig. 4). The
 122 radius of this cylinder $r_E = 1.2r_P$ in most models, except for case S2, in which $r_E = 100$ km \approx
 123 $1.33r_P$ (cf. Table 1). The imposed initial volume percent of eclogite within the cylinder is $\Phi_{ECL,SW}$
 124 on the southwestern (SW) side of the plume and $\Phi_{ECL,NE}$ on the northeastern (NE) side, both
 125 varied for different models between 8% and 16% (cf. Fig. 4). With plate motion parallel to the x -
 126 direction, the y -direction is NE-SW. In symmetric cases S1-S2, the imposed distribution of
 127 eclogite is uniform ($\Phi_{ECL,SW} = \Phi_{ECL,NE}$, Fig. 4). For the other models (cases Z1-Z5), a
 128 compositional bilateral zonation in the deep plume stem is simulated by imposing $\Phi_{ECL,SW} >$
 129 $\Phi_{ECL,NE}$. This aspect of our model setup is novel compared to any thermochemical plume study to
 130 date, including *Ballmer et al.* (2013). We note that the end-member situations of purely
 131 axisymmetric (S1-S2) versus bilaterally asymmetric (Z1-Z5) compositional structure are
 132 idealizations of what is probably more complex in reality.

133 In contrast to the eclogitic core ($r \leq r_E$) of the plume, the relatively cool plume outskirts ($r >$
 134 r_E) with excess temperatures $< \sim 110$ K (case S2: $< \sim 87$ K), as well as the cooler ambient mantle
 135 contain no eclogite. Both the plume and the ambient mantle are dominated by peridotitic
 136 lithologies: they initially contain $\Phi_{HP} = 20\%$ hydrous peridotite in addition to the percentage Φ_{DP}
 137 $= (100\% - \Phi_{HP} - \Phi_{ECL,SW})$ of dry peridotite. The remainder of the mantle consists of a refractory
 138 lithology that does not melt beneath the hotspot (cf. Stracke et al., 2011). Accordingly, the initial
 139 volume fraction of the refractory lithology is $\Phi_{RL} = \Phi_{ECL,SW}$ in the ambient mantle, $\Phi_{RL} = 0\%$ on
 140 the SW side of the deep plume stem, and $\Phi_{RL} = \Phi_{ECL,SW} - \Phi_{ECL,NE}$ on the NE side. Composition
 141 is advected with the flow, evolves due to melting and hybridization (see next paragraph) and is
 142 steadily replenished (and set to initial conditions) where material enters the model domain at the
 143 front side of the model box and the base of the plume.

144 Including eclogite in the models impacts the results both through the associated variations in
 145 the mantle density due to solid phase changes and melting (Fig. 2), as well as the expression of

146 mafic material in the magmas. To account for the effects of phases changes in the quartz and
147 olivine systems, the excess density of eclogite relative to peridotite is defined to be 220 kg/m^3 in
148 the depth range 300 to 410 km, and 110 kg/m^3 elsewhere, based on the laboratory experimental
149 results of *Aoki and Takahashi* (2004). For eclogite melting, we use *Yasuda et al.*'s (1994)
150 empirically-derived parameterization. As such, the models predict eclogite to begin melting first
151 at a depth of ~ 260 km and continue to melt to a maximum allowable extent of 60% at a depth of
152 ~ 150 km within the hottest core of the plume (Sobolev et al., 2005; 2011). We assume that once
153 any eclogitic melt is formed, it instantaneously reacts with the ambient peridotite in a 1-to-1
154 fashion to form biminerally, olivine-free pyroxenite (Yaxley and Green, 1998; Sobolev et al.,
155 2005; 2007; Herzberg, 2011). In the hotspot melting zone at about 110-200 km depth, both
156 peridotite and pyroxenite melt, and do so according to the parameterizations of *Hirschmann*
157 (2000) and *Pertermann and Hirschmann* (2003), respectively. Further details of the melting
158 parameterization, as well as of the mantle density and rheology treatments are reported in the
159 Appendix. Model parameters are listed in Table 2.

160 Following *Ballmer et al.* (2010, 2011; 2013), the predicted volumetric fraction X_{PX} of
161 pyroxenite-derived to the total (i.e., pyroxenite + peridotite derived) volume of volcanism is the
162 quantity used to characterize lava composition. This quantity is computed by assuming all
163 magmas rise vertically and mix perfectly before reaching the surface. To predict the average
164 composition of shield-stage volcanism on the SW and NE sides of the hotspot (i.e., $X_{PX,SW}$ and
165 $X_{PX,NE}$, respectively), we integrate over two adjacent, rectangular strips on the surface. Each strip
166 is 80 km long in the x -direction (i.e., parallel to plate motion) and 63.4 km wide in the y -
167 direction, thus the total width (in y) of the rectangular zone, from which extracted magmas are
168 focused to form the double volcano chain, is 126.8 km. To capture main shield-stage volcanism
169 (of duration $\tau_{shield} \approx 1$ Myr) along the two (i.e., Kea and Loa) volcano trends the two strips (of
170 length $80 \text{ km} = \tau_{shield}/v_{plate}$) are positioned to maximize the total volcanic flux between them with
171 similar fluxes from each strip. Accordingly, the boundary between the two strips nearly bisects
172 the absolute peak in vertical magma flux from below, and defines the central axis of the model
173 hotspot chain. It is this axis that is used to define bilateral symmetry or asymmetry of plume
174 parameters and volcanism.

175

176 3. Results

177 The models are relevant to the Hawaiian hotspot in that their predictions are consistent with
178 key observations. In all our models (cf. Table 1), a hot mantle plume rises through the upper
179 mantle to support localized hotspot (i.e., shield-stage) volcanism, focused over an area ~ 100 km
180 long and ~ 75 km wide — consistent with geological constraints. The plume thermal anomaly
181 imposed at the base of the model of +300 K agrees well with chemical geothermometry
182 (*Herzberg et al.*, 2007). From case to case, the predicted average volcanic flux varies between
183 $\sim 130,000 \text{ km}^3/\text{Myr}$ and $\sim 190,000 \text{ km}^3/\text{Myr}$ (or $\sim 4.1 \text{ m}^3/\text{s}$ and $\sim 6.0 \text{ m}^3/\text{s}$, see Table 3), a range

184 that is within that of published measurements (van Ark and Lin, 2004; Vidal and Bonneville,
185 2004; Robinson and Eakins, 2006). The modeled plumes also dynamically push up the plate to
186 support hotspot swells of heights $870 \text{ m} \leq h_{swell} \leq 960 \text{ m}$ and widths $1130 \text{ km} \leq w_{swell} \leq 1340 \text{ km}$
187 — similar to observations (Wessel, 1993; Crosby and McKenzie, 2009) (also see arch-shaped
188 region of shallow seafloor around Hawaii in Fig. 1). As the amount of mafic materials carried by
189 the plume varies from case to case, we modulate plume radius to maintain good agreement with
190 these key hotspot characteristics (Table 1).

191 One result common to all of the models is that mafic lithologies heavily contribute to hotspot
192 volcanism. Any eclogite carried by the plume, of which the initial contents in our models vary
193 between 8% and 16% from case to case (and from side to side of the plume), melts to a
194 maximum degree of 60% in the depth range of about 150-260 km to react with ambient
195 peridotite (in a 1:1 fashion) and to form pyroxenite (Yaxley and Green, 1998; Sobolev et al.,
196 2005; 2007). The resulting moderate fractions of pyroxenite (i.e., 9.6%-19.2% of the mantle)
197 dominate magmatism, contributing $X_{PX} > 50\%$ ($66\% < X_{PX} < 83\%$) to the model hotspot lavas,
198 even though the source consists mainly of peridotite (with volume fractions of 74.4%-87.2%).
199 This dominance is caused by the much higher isobaric melt productivities in pyroxenite than in
200 peridotite, and reinforced by consumption of latent heat by the first at the expense of the latter
201 (Phipps Morgan, 2001; Katz and Rudge, 2011). While such a dominance of melting mafic
202 materials at the Hawaiian hotspot is indeed supported by many recent studies (Hauri, 1996;
203 Huang and Frey, 2005; Sobolev et al., 2005, 2007; Huang et al., 2007; Herzberg, 2011; Jackson
204 et al., 2012; Pietruszka et al., 2013), other studies favor a dominance of peridotitic melting (cf.
205 Putirka et al., 2011). We also note that our predictions in terms of X_{PX} are upper bounds, as
206 incomplete wall-rock reactions in the deep eclogite melting zone can produce mafic lithologies
207 with lower productivities than simulated in this study (e.g. websterites instead of pyroxenites
208 (Mallik and Dasgupta, 2012)).

209

210 3.1 Double layering of plume material in the upper mantle

211 The presence of dense eclogite leads to thermochemical plumes that are wider and rise more
212 sluggishly compared to non-eclogitic (i.e., thermal or “classical”) plumes with similar thermal
213 buoyancy fluxes. Moreover, the doubling of the excess density of eclogite in the depth range of
214 300 to 410 km due to the effects of phase transitions in the quartz and olivine systems (Aoki and
215 Takahashi, 2004) can profoundly modify plume morphologies and upwelling dynamics (cf.
216 Ballmer et al., 2013). If enough eclogite is present in the deep plume conduit (see below) the rise
217 of the plume partially stalls in this depth range to form a layer of hot material hundreds of km
218 wide and ~150 km thick (Fig. 5), which we refer to as the deep eclogitic pool (DEP).

219 For example, in cases S1-S2, the eclogitic plume core (originally 15% eclogite) has a net
220 (i.e., thermal plus compositional) buoyancy of -3.3 kg/m^3 to about -23 kg/m^3 within the critical

221 depth range of 410-300 km, imaged as the blue region in Figs. 5b,e (buoyancy is defined as the
222 density deficit relative to the ambient mantle at the reference temperature). Accordingly, this
223 material tends to sink back down into the transition zone. However, it is supported from below
224 by the deep plume conduit (red colors at the bottom of Figs. 5b,e), which in the transition zone is
225 almost entirely positively buoyant (i.e., by up to $\sim+13.2$ kg/m³), and is sustained on its sides by
226 the non-eclogitic plume outskirts (with a buoyancy of up to $\sim+10$ kg/m³; red sheath around the
227 blue DEP in Figs. 5b,c,e,f). Therefore, the eclogitic core spreads laterally (but not indefinitely) to
228 form a wide DEP (Figs. 5a-f). As material continues to feed the DEP from below, the DEP
229 inflates to cross the 300 km-deep coesite-stishovite phase transition, where the material
230 instantaneously regains a positive net buoyancy (Figs. 5c,f). The resulting increase in upwelling
231 rate above this phase transition sets up a local minimum in dynamic pressure that guides the (not
232 necessarily vertical) rise of material through the DEP. This local minimum is enhanced by the
233 consumption of eclogite due to melting, occurring in the depth range of about 150-260 km. This
234 process strongly enhances the net buoyancy. Consequently, the shallow plume conduit is
235 narrower and rises more rapidly (by rates of up to ~ 1 m/yr) than the deep plume stem, and ponds
236 beneath the lithosphere as a thin (<100 km) pancake that supports the hotspot swell.

237 Similarly, compositionally-zoned cases Z3-Z5 with average eclogite contents >12% display a
238 strong double layering of plume material with a wide DEP (Figs. 5m-u). In these cases, material
239 from the more eclogite-rich, SW sides of the plumes primarily inflates the DEP as shown in Figs.
240 6d-f by contours of initial eclogite content (i.e., eclogite content with any modifications due to
241 melting removed). The materials from the eclogite-poor NE sides of the plumes instead rise
242 relatively rapidly through, and contribute relatively little volume to the DEP, as they largely
243 remain positively buoyant (by up to $+3.3$ kg/m³ (case Z3) and $+7.7$ kg/m³ (case Z5)).

244 In contrast, in compositionally-zoned cases Z1-Z2 with average eclogite contents <12%,
245 most of the plume-core material remains positively or near-neutrally buoyant even in the depth
246 range of 300-410 km. The plumes therefore rise without stalling significantly to form a DEP
247 (Figs. 5g-l). Just a portion of the cooler outer plume core in case Z2, particularly on the SW side,
248 becomes marginally negatively buoyant, leading to only a slight ($\sim 50\%$) widening of the plume
249 conduit in the mid upper mantle (Fig. 5k). The plume dynamics in cases Z1 and Z2 are indeed
250 much like that of a classical thermal plume (Figs. 5g-l).

251 In summary, average initial plume-core eclogite contents >12% appear to be required to form
252 a DEP in plumes with parameters that are realistic for the Hawaiian Plume (see above). As the
253 dynamical behavior is governed by the competition of thermal and compositional buoyancy
254 forces, smaller such contents would be required for other plumes with smaller excess
255 temperatures (Herzberg et al., 2007). For example, a content of >6% is likely to be sufficient to
256 induce formation of a DEP for a perhaps more common plume with a peak excess temperature of
257 ~ 150 K. The estimated critical eclogite contents would have to be slightly corrected upward (by
258 $\sim 3\%$) if the ambient mantle itself contained eclogite ($\sim 3\%$), as is indicated by studies of mid-
259 ocean ridge basalts that suggest a content of $\sim 5\%$ pyroxenite in the upper mantle (Hirschmann

260 and Stolper, 1996). Considering this possibility, the eclogite contents modeled here can be
261 regarded as excess contents relative to the ambient mantle.

262

263 3.2 Asymmetry in plume behavior and melting

264 Our models not only display complex and asymmetric structures at the depths of the DEP (i.e.,
265 410-300 km), but also above this depth range (Fig. 6). These asymmetries are seen in the overall
266 morphology of the plume as a whole, as well as in the temperatures and eclogite contents across
267 the shallow plume conduit and plume pancake (section 3.2.1). The structure of temperature and
268 initial eclogite content (i.e., eclogite content imposed in the deep plume stem) within the melting
269 zone are then found to produce bilateral asymmetries in the mafic contribution to volcanism
270 (section 3.2.2). Despite these asymmetries, the current models generally reproduce the main
271 results of purely thermal plume models (Farnetani and Hofmann, 2009; 2010; Farnetani et al.,
272 2012) that materials originating from distinct sides of the deep plume stem mostly remain on
273 their sides all the way to the surface (evident in contours of initial eclogite content, Fig. 6).
274 However, the added effects of compositional buoyancy as well as melting behavior of peridotitic
275 vs. mafic material in our models lead to different conclusions about the relationship between
276 magma and source compositions.

277

278 3.2.1 Thermochemical-plume dynamics, temperature, and composition

279 In case Z3, strong asymmetry in temperature rises out of a compositionally-zoned deep
280 plume stem and DEP (Fig. 6). The higher imposed eclogite content on the SW versus the NE
281 side of the deep plume core ($\Phi_{ECL,SW} = 15\%$, $\Phi_{ECL,NE} = 12\%$) leads to a higher average excess
282 density on the SW side, a density contrast that doubles in the depth range of 300-410 km where
283 the DEP forms. This situation has three important consequences: First, the NE side of the DEP
284 (with a near-neutral average buoyancy of about -0.9 kg/m^3) is preferentially entrained into the
285 shallow plume, whereas the SW side of the DEP (with a strongly negative average buoyancy of
286 about -9.7 kg/m^3) displays more extensive pooling and lateral spreading (see contours in Fig.
287 6d). Second, the more eclogitic material from the SW side of the deep plume stem, fills over half
288 of the DEP (imaged as broad orange-to-yellow area in Fig. 7m), pushing the less eclogitic
289 material as well as the whole shallow plume conduit to the NE (dashed-dotted line in Fig. 6d is
290 symmetry axis of the model setup for reference). Third, the less hot, outer plume-core material
291 from the SW side of the deep plume stem fails to rise through the depth range of 300-410 km
292 (green colors on the right-hand side of Fig. 6d; dark blue colors Figs. 5n-o). Therefore, the
293 materials that enter the shallow plume from the (initially more eclogitic) SW side are, on
294 average, hotter than those on the (initially less eclogitic) NE side. The variations in initial
295 eclogite content in the DEP thus create a “thermal filter” for the temperatures entering the
296 shallow plume. The resulting thermal asymmetry in the shallow plume conduit is visualized in

297 Figure 7 (m-o) as an offset between the peak in temperature (bull's eye of dark grey contours;
298 black cross) and the focus in mantle upwelling (bull's eye of red contours; red cross). As the
299 focus of upwelling lies very close to the peak hotspot volcanic flux, which defines the hotspot
300 location, case Z3 predicts bilateral asymmetry with higher temperatures on the SW side of the
301 hotspot melting zone (green and black dashed lines encircle the pyroxenite + peridotite melting
302 zone in Fig. 6d with colors highlighting the thermal asymmetry).

303 Increasing the contrast in initial eclogite contents of the deep plume stem (from case Z3 to
304 cases Z4 and Z5) boosts the asymmetry in the make-up and temperature distribution of the
305 shallow plume conduit. The modeled plumes in cases Z4 and Z5 carry average eclogite contents
306 (Table 1) that are similar to those of case Z3, and therefore generally behave similarly to that in
307 case Z3. However, they display greater cross-chain variations in initial eclogite contents (Table
308 1). As the thermal-filter effect is greater, the proportion of the less eclogitic (NE) relative to the
309 more eclogitic (SW) material within, as well as the thermal asymmetry across the shallow plume
310 conduit increase from cases Z3 to Z4, and Z4 to Z5 (preponderance of green and blue colors
311 increases from Fig. 7o to Fig. 7r to Fig. 7u). The asymmetry of the overall morphology of the
312 plume also increases with greater initial eclogite contrast (Figs. 5m-5u), as the less eclogitic, NE
313 material, which predominantly feeds the shallow plume, is pushed increasingly to the margins of
314 the DEP (Fig. 7). Accordingly, the offset between the peak temperature and the peak upwelling
315 rate increases from cases Z3 (~15 km) to Z5 (~40 km).

316 In contrast to cases Z3-Z5, cases Z1-Z2 do not display significant thermal asymmetry of the
317 shallow plume (Fig. 7) despite a deep-rooted compositional asymmetry that differs only slightly
318 from that in case Z3 (In cases Z1, Z2 and Z3, $\Phi_{ECL,SW}$ equals $1.25\Phi_{ECL,NE}$, $1.2\Phi_{ECL,NE}$, and
319 $1.25\Phi_{ECL,NE}$, respectively; cf. Fig. 4). The main cause for the lack of the asymmetry is the lack of
320 a large DEP in cases Z1 and Z2. Accordingly, plume material rises rapidly through the depth
321 range of 300-410 km, the thermal filter effect (as discussed above for cases Z3-Z5) is negligible,
322 and any thermal asymmetry of the shallow plume conduit relative to the peak upwelling rate (and
323 hence hotspot center) is minimal (Fig. 7).

324 For a non-zoned plume, any thermal asymmetry across the shallow plume conduit would
325 have to be explained by entirely different mechanisms than those described above, as the make-
326 up of the deep plume stem in these cases is axisymmetric (with 15% eclogite throughout the
327 plume core). While case S1 displays only very minor thermal asymmetry of the shallow plume,
328 case S2 displays strong asymmetry – both across the DEP and the shallow plume (Figs. 5-7). In
329 both cases, the DEP is strongly negatively buoyant (average buoyancy is about -10 kg/m^3 , cf.
330 Table 1) and is again prevented from sinking down into the lower mantle by the rise of the deep
331 plume stem from below (and is contained laterally by the non-eclogitic plume outskirts rising
332 around its sides). Such a quasi-stable DEP is sensitive to ambient-mantle flow such as that
333 induced by sublithospheric small-scale convection (Ballmer et al., 2007; 2011) or ambient
334 mantle wind (cf. Steinberger and Antretter, 2006). In the current calculations, a sublithospheric
335 downwelling interacts with the plume pancake and leans down on the NE side of the DEP (Figs.

336 5 and 6). In case S1, this downwelling is insufficient to induce strong dynamical asymmetry
 337 within the DEP, as the DEP is well supported from the sides by a relatively thick and buoyant
 338 layer of plume-outskirt material (Figs. 5b,c). In case S2, the sublithospheric downwelling is
 339 instead sufficient to displace the whole DEP and to cause the shallow plume conduit to rise off-
 340 center (i.e., from the DEP on the side opposite to the downwelling), as the supporting layer of
 341 plume-outskirt material is thinner and less buoyant (Figs. 5e,f). Such an off-center rise (i.e.,
 342 shifted to the SW) causes an asymmetric temperature distribution in the shallow plume with
 343 higher temperatures on its NE side. That said, the thermal gradient across the shallow plume in
 344 case S2 is opposite to that in cases Z3-Z5 (i.e., with higher temperatures on the SW side). We
 345 note however that the SW and NE directions are conventions of our model setup defined by the
 346 distribution of eclogite in the deep plume stem (with $\Phi_{ECL,SW} \geq \Phi_{ECL,NE}$), and that models S1 and
 347 S2 with $\Phi_{ECL,SW} = \Phi_{ECL,NE}$ may be mirrored about the central plane at $y = 1650$ (mirrored cases
 348 Z1-Z5 would have $\Phi_{ECL,SW} < \Phi_{ECL,NE}$).

349 The temperature distribution across the shallow plume in case S2 is not only asymmetric, but
 350 is also time-dependent (Figs. 6g-h). Such time-dependence is related to episodic extraction of hot
 351 material out of the DEP. Any extraction tends to increase the net density of the DEP. In case S2,
 352 this increase is sufficient to cause the DEP to spread laterally and sink slightly, a process that
 353 chokes the flux of material through the DEP's roof. Once outflow is smaller than inflow from
 354 below, the DEP re-inflates, until it is thick enough for material to rise above the coesite-
 355 stishovite phase transition at 300 km depth to generate another shallow-plume pulse (also see
 356 Movie S3 in Ballmer et al., 2013). The process begins again, and resulting shallow-plume
 357 pulsations provide a dynamical explanation for the variations in total volcanic flux documented
 358 along the Hawaii-Emperor chain (van Ark and Lin, 2004; Vidal and Bonneville, 2004; Ballmer
 359 et al., 2013). In addition, the location of the shallow plume meanders relative to the DEP creating
 360 a time-dependence of the average temperature and thermal asymmetry across the shallow plume
 361 conduit. In cases S1 and Z1-Z5 instead, the DEP is sufficiently well supported by plume-outskirt
 362 material (due to small r_E) to balance inflow and outflow. Thus, an increase of the eclogitic plume
 363 core's radius, r_E from 90 to 100 km controls the regime shift between the pseudo-steady case S1
 364 and strongly time-dependent case S2 (cf. Ballmer et al., 2013). Accordingly, we expect that
 365 double-layered, compositionally-zoned plumes with $r_E \approx 100$ km also display shallow-plume
 366 pulsations.

367

368 3.2.2 Melting dynamics and its expression in volcanism

369 In our models, a combination of thermal asymmetry across the melting zone and
 370 compositional zonation of the plume conduit gives rise to geographical variations in hotspot-lava
 371 composition. In cases Z1-Z2, temperatures across the melting zone are only minimally
 372 asymmetric, therefore, the source composition advected from the deep plume stem
 373 predominantly controls magma make-up. Accordingly, the contribution of pyroxenitic lavas in

374 volcanism X_{PX} is higher on the SW side of the hotspot as it overlies higher eclogite contents in
 375 the plume stem (Figs. 8c-d, Table 3). This prediction agrees with the traditional explanation for
 376 geographical variations in lava composition, particularly for the Hawaiian Kea and Loa trends
 377 (Abouchami et al., 2005; Farnetani and Hofmann, 2009; 2010; Huang et al., 2011; Weis et al.,
 378 2011; Farnetani et al., 2012). However, cases Z1 and Z2 suffer from a key weakness: the plumes
 379 do not develop a broad DEP, and thus cannot explain the seismic structure imaged by the
 380 PLUME regional seismic tomography (see next section).

381 The relationship between magma and plume-stem make-up differ for the compositionally-
 382 zoned cases which do produce a DEP (Z3-Z5). These are the cases with strong thermal
 383 asymmetry in the shallow plume (see section 3.2.1), and results show that peridotite melting
 384 starts deeper (Figs. 6d-6h) and reaches higher degrees on the hotter side of the shallow plume
 385 conduit than on its cooler side. The effect of thermal asymmetry on pyroxenite melting is much
 386 smaller, as pyroxenite reaches maximum degrees of melting on both sides. These melting
 387 dynamics systematically reduce X_{PX} on the hotter (and more eclogitic) SW side of the hotspot
 388 (Figs. 8e-g), and accordingly trade off with the effects of source composition in terms of X_{PX} .

389 In case Z4, for example, the shallow thermal asymmetry consequently leads to a more-or-less
 390 symmetric distribution of X_{PX} across the main melting zone thus completely obscuring the
 391 bilateral asymmetry in the composition of the plume conduit (Fig. 8f, Table 3). In cases Z3 and
 392 Z5, the effect of thermal asymmetry on melting dynamics even reverses the sense of bilateral
 393 asymmetry in magma composition compared to the plume's compositional zonation (Figs. 8e,g).
 394 In case Z3, the average X_{PX} is greater on the NE side with $X_{PX,SW} - X_{PX,NW} = -1.2\%$ despite the fact
 395 that it is the SW side of the plume that contains more eclogite initially ($\Phi_{ECL,SW} - \Phi_{ECL,NE} =$
 396 $+3\%$). Case Z5 predicts an even greater reversal in asymmetry at the surface ($X_{PX,SW} - X_{PX,NE} \approx -$
 397 9%), although it has the strongest bilateral asymmetry in the deep conduit ($\Phi_{ECL,SW} - \Phi_{ECL,NE} =$
 398 $+6\%$) of the cases modeled. Thus, the thermal asymmetry of the material feeding the melting
 399 zone can be as important or even more important than the zonation in the deep plume stem in
 400 controlling the geographic patterns of X_{PX} .

401 In fact, thermal asymmetry alone can give rise to geographic variations in lava composition
 402 even without any compositional zoning in the deep plume stem (Ballmer et al., 2013). In case S2,
 403 both $X_{PX,SW}$ ($\sim 83.4\%$ to $\sim 91.5\%$) and $X_{PX,NE}$ ($\sim 79.0\%$ to $\sim 90.8\%$) strongly vary over model time
 404 (Figs. 8h-j; Table 3), both due to temporal variations in the flux of and lateral variations in
 405 temperature within the shallow plume conduit (Figs. 6g-h; also see last paragraph of section
 406 3.2.1). Although the initial eclogite content in case S2 remains constant across the plume core,
 407 X_{PX} generally remains lower on the (hotter) NE side of the hotspot than the (cooler) SW side,
 408 except for a very few snapshots with near-symmetric X_{PX} , one of which is shown in Figure 8h.
 409 The difference in average X_{PX} between the two sides (i.e., $X_{PX,SW} - X_{PX,NE}$) ranges between $\sim 0.6\%$
 410 and $\sim 6.8\%$. Case S1 with near-symmetric temperatures in the shallow plume instead does not
 411 display significant asymmetry in X_{PX} across the hotspot (Fig. 8a, Table 3).

412

413

3.3 Implications of seismic constraints on plume dynamics

414 To compare our model predictions with geophysical constraints from seismic tomography,
415 we compute three-dimensional models of synthetic seismic shear-wave velocity from our
416 geodynamic simulations. Synthetic seismic velocities are calculated from the temperatures,
417 densities and eclogite contents predicted from our simulations. We use the method of *Faul and*
418 *Jackson (2005)* to do this computation (for parameters used, see *Ballmer et al., 2013*), and
419 account for the effects of eclogite content on seismic velocities according to *Xu et al. (2008)*. For
420 comparison, we also predict a synthetic seismic velocity model for a purely thermal plume (i.e.,
421 based on the reference model of *Ballmer et al. (2011)*).

422 Figure 9 shows horizontal cross-sections through the synthetic velocity models at 350 km
423 depth, and elucidates that the models fall into two categories: first, models with a wide body of
424 seismically slow material in the mid upper mantle (cases S1-S2, Z3-Z5) due to the presence of a
425 DEP; second, models without such a wide low-velocity body (cases Z1-Z2), similar to the
426 reference thermal (i.e., classical) plume model (Fig. 9a). Only plumes from the first category are
427 able to stabilize large volumes of seismically slow material in the upper mantle. We note that
428 Figure 9 shows a forward model of synthetic seismic velocities, unfiltered by the inversion
429 process. Seismic filtering (i.e., by a resolution test) would instead be required to directly compare
430 these velocity models to seismic tomography images, particularly for vertical cross-sections (not
431 shown in Figure 9), in which biases of the inversion process (such as smearing) are expected to
432 be most strongly expressed.

433 Using the inversion matrix of the shear-wave tomography model of *Wolfe et al. (2009)*,
434 *Ballmer et al. (2013)* performed such seismic resolution tests for case S1 (Fig. 9b) and the
435 reference thermal plume model (Fig. 9a), representative cases for the first and second (with and
436 without DEP) categories, respectively. These tests demonstrated that the double layering of
437 plume material as in our case S1 (i.e., analogous to their case A) is expected to be imaged as one
438 thick (~400 km) and wide (~500 km) body of low velocities (due to vertical smearing), much
439 like what shear-wave tomography imaged beneath Hawaii (*Wolfe et al., 2009*). They further
440 showed that our case S1 can provide a much better explanation for the station-averaged, shear-
441 wave arrival times measured during the seismic PLUME experiment than the reference thermal
442 plume model (originally from *Ballmer et al. (2011)*). Accordingly, manifestation of a DEP
443 beneath the Hawaiian hotspot such as in cases S1-S2 and Z3-Z5 is demanded by the seismic
444 constraints.

445 This interpretation is supported by joint inversion of surface-wave, shear-wave and ambient-
446 noise data collected during PLUME. Such a joint inversion (Fig. 3; *Cheng et al. (this volume)*)
447 resolves more detailed structure within the large body of low velocities retrieved from shear-
448 wave tomography alone (*Wolfe et al., 2009*). It suggests the presence of two distinct layers of
449 seismically slow material at the predicted depths of the DEP and plume pancake. This

450 geophysical evidence points toward a thermochemical plume beneath Hawaii much like those
451 portrayed in this study (i.e., in cases S1-S2, Z3-Z5), and away from a more classical plume
452 without a DEP (cases Z1-Z2).

453 On a more detailed level, the predictions of the subset of our models with a DEP also appear
454 to be in good agreement with the specific structures resolved by joint tomography. In terms of its
455 lateral extent, the predicted body of seismically slow material (i.e. DEP) in a subset of our
456 models (especially, S1, S2, Z3-Z5) is consistent with observations (dashed ellipses in Fig. 9 and
457 3e), albeit displaced eastward. The presence of short-wavelength, seismically fast structure
458 within the DEP, as predicted by cases S2 and Z5 (Figs. 9c, 9h), is also generally consistent with
459 observations (cf. Fig. 3e). These first-order agreements between predictions of simplified
460 geodynamic models and geophysical constraints are indeed encouraging.

461

462 **4. Discussion**

463 In our geodynamic study, we find three different scenarios for geographic variations in the
464 materials melting beneath the hotspot: (1) Cases without a DEP (Z1 and Z2) predict a direct
465 geometrical relationship between the geographic pattern of mafic content in volcanism (X_{PX}) and
466 the zonation of the deep plume conduit, similar to the traditional explanation for the geochemical
467 differences between the Loa and Kea trends (Abouchami et al., 2005; Farnetani and Hofmann,
468 2009; 2010; Huang et al., 2011; Weis et al., 2011; Farnetani et al., 2012). (2) In contrast,
469 compositionally-zoned cases with a DEP (cases Z3-Z5) predict a non-intuitive relationship, as
470 thermal asymmetry across the shallow plume conduit boosts peridotite melting on the more
471 eclogitic side to veil (Z4) or even reverse (Z3 and Z5) the asymmetry of mafic materials in
472 volcanism. (3) Finally, thermal asymmetry is sufficient to generate a geographic asymmetry in
473 X_{PX} even for non-zoned plumes (case S2).

474 Of these three scenarios, only scenarios 2 and 3, which include a DEP, are applicable to
475 Hawaii. Only they can account for the stabilization of large volumes of hot, seismically slow
476 material in the mid upper mantle, as is indicated by the PLUME tomography results (cf. Wolfe et
477 al., 2009; Ballmer et al., 2013). Thus, shallow thermal asymmetry rising out of the DEP (as in
478 scenarios 2 and 3) appears to be as or more important than a deep compositional zonation of the
479 plume (as only in scenario 2) in giving rise to the geochemical difference between the Hawaiian
480 Kea and Loa trends. In both scenarios 2 and 3, the low- X_{PX} side of the melting zone is predicted
481 to be hotter (thus peridotite melts to higher extents) than the high- X_{PX} side. As Kea-type lavas are
482 thought to be influenced less by mafic melting than Loa-type lavas (i.e., $X_{PX,SW} > X_{PX,NE}$ (Sobolev
483 et al., 2005; Greene et al., 2010; Herzberg, 2011; Jackson et al., 2012)), we infer that the Kea
484 side of the mantle melting zone is hotter than the Loa side (cf. Xu et al., in press). Accordingly,
485 the distinction between the Kea and Loa trends can either arise out of a non-zoned Hawaiian
486 Plume (scenario 3) (cf. Ballmer et al., 2011; 2013), or a zoned plume with greater eclogite

487 contents on the low- X_{PX} Kea side of the deep plume stem (scenario 2) — not on the high- X_{PX} Loa
488 side as previously inferred (e.g., Sobolev et al., 2005). In either case, the model results in
489 combination with the seismic evidence, argue against a direct geographic link between Loa and
490 Kea lava geochemistry and the composition of the SW and NE sides of the deep plume stem (cf.
491 Abouchami et al., 2005; Farnetani and Hofmann, 2010; Huang et al., 2011; Weis et al., 2011).

492 Future studies should be designed to distinguish between scenarios 2 and 3, and hence to test
493 whether the deep Hawaiian Plume is indeed compositionally zoned. Thermal asymmetry across
494 the melting zone is greater in scenario 2 than in scenario 3, and greatest in the cases with the
495 strongest contrast in initial plume eclogite content (i.e., case Z5 in this study). Differences in
496 temperature between the two sides control variations in the maximum extent of peridotite
497 melting across the hotspot, which should be testable using major elements and various trace-
498 elements. The challenge here will be to distinguish the contributions from mafic versus
499 peridotitic melting, which are expected to be sensitive to temperature themselves. Such a test will
500 hence likely require a combination of geodynamic modeling with targeted geochemical analysis.
501 Geophysical evidence may be able to provide complementary constraints on the amplitude of
502 asymmetry in temperature across the melting zone (cf. Rychert et al., 2013), and thus ultimately
503 on that in eclogite content across the plume stem.

504 Constraining the make-up of the plume stem feeding into the DEP will serve to improve our
505 understanding of the behavior of the plume in the lower-mantle. Geodynamic models have
506 predicted complex thermochemical plume dynamics for a range of compositions involving
507 plume pulsations on timescales of 10s of Myr, or longer (e.g., Lin and van Keken, 2005;
508 Kumagai et al., 2008). Such pulsations would be superimposed on mid-term pulsations rising out
509 of the DEP itself such as predicted by our study (e.g., case S2). These long-term and mid-term
510 pulsations ultimately act to modulate the compositions and temperatures across the melting zone,
511 and are thus able to address the time-evolution of the Loa/Kea geochemical asymmetry, which
512 may (Sinton et al., in review) or may not (e.g., Abouchami et al., 2005) persist up the chain
513 beyond the Molokai Fracture Zone (cf. Fig. 1). We also note that there is no direct evidence for
514 or against the existence of a DEP beneath the Hawaiian hotspot 10s of Myr ago. While crustal
515 thickness variations along the Hawaii-Emperors (van Ark and Lin, 2004; Vidal and Bonneville,
516 2004) on timescales that are consistent with DEP pulsations may be taken as indirect evidence
517 (cf. Ballmer et al., 2013), future geodynamic studies should assess the long-term stability of a
518 DEP, especially with strongly time-dependent plume behavior in the lower mantle feeding into
519 the DEP.

520 Resolving the dynamics and melting of the Hawaiian Plume in space and time is indeed
521 needed to improve our understanding of the mantle as a whole. For example, it may provide
522 insight into the compositions of the materials making up the deep lower mantle, as well as the
523 dynamical processes by which the Hawaiian Plume may or may not entrain LLSVP material (cf.
524 Steinberger and Torsvik, 2012). Studying other plumes in addition to the Hawaiian Plume may
525 provide constraints on the heat and material fluxes across the mantle, as well as the possible

526 origins of the LLSVPs. However, our results suggest that high-resolution seismic images of these
527 other plumes would be required to assess the origin of any local-scale geographic variations in
528 lava geochemistry across the related hospots.

529

530 **5. Conclusions**

531 In this study, we examine the upper-mantle dynamics of mantle flow and melting of
532 thermochemical plumes with a bilateral zonation in the content of mafic materials rising out of
533 the lower mantle. The predictions of our geodynamic simulations can be grouped within three
534 different scenarios:

- 535 (1) Thermochemical plumes with a bilateral asymmetry in eclogite content, and average such
536 contents of <12%, behave similar to classical thermal plumes with little mixing between
537 the two sides of the plume and a direct relationship between source and lava composition,
538 consistent with previous findings (Farnetani and Hofmann, 2009; 2010). However, these
539 plumes cannot account for the stabilization of large volumes of hot material in the mid
540 upper mantle, as is evident for the Hawaiian Plume by seismic tomography.
- 541 (2) In contrast, compositionally-zoned plumes with average eclogite contents of >12%
542 intermittently stagnate in the depth range of about 300-410 km to form a deep eclogitic
543 pool (DEP), and hence can reconcile seismic constraints. This pooling is due to a relative
544 density maximum of eclogite at these depths, which in turn only allows the hottest
545 material to enter the shallow plume on the more eclogitic side of the plume. The resulting
546 thermal asymmetry across the melting zone gives rise to more vigorous peridotite melting
547 on the initially more eclogitic side, therefore reducing the expression of mafic materials
548 in volcanism X_{PX} to the point that it is similar to or even lower than on the other (i.e.,
549 initially less eclogitic) side.
- 550 (3) Moreover, compositionally non-zoned plumes that rise asymmetrically out of a DEP
551 (e.g., due to ambient mantle flow) can also sustain a thermal gradient across the melting
552 zone, and thus geographic variations in X_{PX} across the hotspot.

553 These model predictions (i.e., scenarios 2 and 3) have important implications for Hawaiian
554 Plume dynamics and the composition of the deep mantle. Asymmetry in X_{PX} across the hotspot,
555 as evident by the geochemical distinction between the Kea and Loa trends (e.g., Sobolev et al.,
556 2005), is not necessarily an explicit indication of a (bilateral) compositional zonation of the deep
557 plume stem, but rather of a thermal gradient across the hotspot melting zone with higher
558 temperatures on the Kea side. If a zonation in the content of mafic materials indeed exists, our
559 results suggest that it is the NE Kea side of the deep plume stem that contains more eclogite than
560 the SW Loa side, contrary to previous interpretations. Our findings put into question previous
561 efforts of mapping the deep mantle from geographical variations in hotspot lava composition.

563 **Table 1:** Key plume parameters and average densities of the plume core for all cases. Radii of
 564 the plume's thermal and compositional anomalies (r_P and r_E) as well as initial eclogite contents
 565 on either side of the plume ($\Phi_{ECL,NE}$ and $\Phi_{ECL,SW}$) are given. Positive and negative net buoyancies
 566 refer to plume-core material being less and more dense than the ambient non-plume mantle,
 567 respectively. Cases S1 and S2 (*) are analogous to cases A and B in *Ballmer et al.* (2013),
 568 respectively.

	r_P	r_E	$\Phi_{ECL,NE}$	$\Phi_{ECL,SW}$	<i>average plume-core net buoyancy</i>	
					<i>at 300-410 km depth</i>	<i>elsewhere</i>
case S1*	75 km	90 km	15%	15%	-9.7 kg/m ³	6.8 kg/m ³
case S2*	75 km	100 km	15%	15%	-10.7 kg/m ³	5.8 kg/m ³
case Z1	65 km	78 km	8%	10%	3.5 kg/m ³	13.4 kg/m ³
case Z2	70 km	84 km	10%	12%	-0.9 kg/m ³	11.2 kg/m ³
case Z3	75 km	90 km	12%	15%	-6.4 kg/m ³	8.4 kg/m ³
case Z4	70 km	84 km	11%	15%	-5.3 kg/m ³	9.0 kg/m ³
case Z5	75 km	90 km	10%	16%	-5.3 kg/m ³	9.0 kg/m ³

569

570

571

572 **Table 2:** notations. ^aHirth and Kohlstedt (1996, 2003); ^bKarato and Wu (1993), ^cHirth
 573 (2002), ^dKohlstedt and Zimmerman (1996); (§) see Appendix 7.2.

Parameter	Symbol	Value
reference ambient mantle temperature	T_m	1350 °C
plume peak thermal anomaly	ΔT_{plume}	300 K
adiabatic gradient	γ	0.3 K/km
heat capacity	c_P	1250 J·kg ⁻¹ ·K ⁻¹
thermal diffusivity	κ	10 ⁻⁶ m ² /s
thermal expansivity	α	3·10 ⁻⁵ K ⁻¹
latent heat of melt	L	560 kJ/kg
critical porosity in peridotite	φ_C	0.4%
critical porosity in pyroxenite	$\varphi_{C,PYX}$	10%
residual porosity in peridotite	φ_R	0.4%
residual porosity in pyroxenite	$\varphi_{R,PYX}$	5%
water partitioning coefficient	D_{H_2O}	0.01
bulk water content in the ambient mantle	c_0	310.64 ppm
water content below which peridotite behaves like dry peridotite ^a	c_{dry}	6 ppm
effective mantle viscosity	η_{eff}	1.6·10 ¹⁹ Pa·s
activation energy ^{b,c}	E^*	300 kJ/mol
activation volume	V^*	5·10 ⁻⁶ m ³ /mol
dehydration stiffening coefficient ^a	ξ	100
melt lubrication exponent ^d	ζ	-40
mantle density	ρ_0	3300 kg/m ³
excess density of eclogite	$\Delta\rho_{ECL}$	110-220 kg/m ³ §
density change with depletion in peridotite	$\Delta\rho_F$	-165 kg/m ³
magma density	ρ_M	2800 kg/m ³
depth of the box	D	660 km
top velocity boundary condition	v_{plate}	80 km/Myr
gravity acceleration	G	9.8 m/s ²
ideal gas constant	R	8.314 Jmol ⁻¹ K ⁻¹

574

575 **Table 3:** Key model predictions for all cases. Swell height h_{swell} ; swell width w_{swell} ;
 576 contribution of mafic lavas in volcanism on the southwestern and northeastern sides of the
 577 hotspot, $X_{PX,SW}$ and $X_{PX,NE}$. (§) Volcanic fluxes reported are average total volcanic fluxes
 578 including secondary volcanism occurring well away from the hotspot. (*) In case S2, the
 579 reported key model predictions strongly vary over model time; the reported values are averages
 580 with standard deviations reported in brackets.

	h_{swell}	w_{swell}	volcanic flux§	$X_{PX,SW}$	$X_{PX,NE}$	$X_{PX,SW} - X_{PX,NE}$
case S1	920 m	1200 km	5.4 m ³ /s	83.56%	82.71%	0.85%
case S2*	732 m (65 m)	1100 km (31 km)	3.4 m ³ /s (0.6 m ³ /s)	87.77% (1.93%)	83.55% (2.34%)	4.22% (1.55%)
case Z1	870 m	1130 km	4.1 m ³ /s	70.49%	65.25%	5.24%
case Z2	940 m	1200 km	6.0 m ³ /s	76.22%	73.54%	-2.68%
case Z3	940 m	1290 km	6.5 m ³ /s	81.32%	82.52%	-1.20%
case Z4	890 m	1190 km	5.5 m ³ /s	66.08%	66.10%	-0.02%
case Z5	960 m	1340 km	5.6 m ³ /s	70.09%	79.04%	-8.95%

581

582

583 6. Figure captions

584

585 **Fig. 1:** Mapview of Hawaiian volcanism and bathymetry. Red and blue triangles denote sites of
 586 Kea-type and Loa-type shield-stage lavas (distinguished by their ²⁰⁸Pb*/²⁰⁶Pb* compositions
 587 (Weis et al., 2011)), respectively. Classifications of Waianae and Kaena-ridge volcanoes are
 588 based on *Sinton et al.* (in review). Yellow triangles mark volcanoes that straddle the dividing line
 589 in ²⁰⁸Pb*/²⁰⁶Pb* as defined by *Abouchami et al.* (2005).

590

591 **Fig. 2:** Conceptual figure (not to scale) of a double-layered, thermochemical plume. The peak in
 592 excess density of eclogite relative to pyrolite (and also relative to peridotite; see left panel as
 593 reproduced from *Aoki and Takahashi* (2004)) can induce stagnation of a thermochemical plume
 594 to as a deep eclogitic pool (DEP) in the depth range of ~300 km to ~410 km. Such a DEP, in
 595 combination with the shallow thermal pancake ponding beneath the lithosphere, place a large
 596 volume of hot and seismically slow material in the upper mantle, which is required by seismic
 597 tomography. The reduction of negative compositional density due to the coesite-stishovite phase
 598 transition at ~300 km depth, as well as due to eclogite melting starting at ~250 km depth pull
 599 eclogitic material out of the DEP in a positive-feedback mechanism.

600

601 **Fig. 3:** Cross-sections through the seismic model HW13-SVJ of *Cheng et al.* (this volume)
602 produced from a joint inversion of shear-wave and surface-wave (teleseismic as well as ambient
603 noise) travel times. The location of the vertical cross-sections in panels (a) and (c) are denoted in
604 the insets in panels (b) and (d) as red lines, respectively (with red and green dots as geographical
605 markers). Black triangles in (b) and (d) show the seismic network used for the inversion. The
606 blue dashed line in (c) approximately separates the Kea and Loa volcano subchains. (e) The
607 horizontal cross-section is located at the same depth (350 km) as the cross-sections through the
608 synthetics shown in Figure 9. Ray coverage is highest within the thin black dashed lines (cf. Fig.
609 6 in *Cheng et al.* (this volume)). A wide body of slow shear-wave velocities at typical DEP
610 depths is segmented by fast structure toward the west, and is surrounded by the pink dashed
611 ellipse. The seismic images show complex structure, crudely consistent with (a) a double-layered
612 plume in the upper mantle and a slanted stem rooted in the lower mantle, (c) a shallow plume
613 that is asymmetric about any axis parallel to plate motion, and (e) a DEP with relatively complex
614 structure. Panels (a) through (d) are reproduced from *Cheng et al.* (this volume) after minor
615 modifications.

616

617 **Fig. 4:** Imposed eclogite content at the base of the deep plume stem for all cases. The eclogite
618 bearing core of the plume is colored black to dark grey, and the surrounding non-eclogitic, but
619 still warm outskirts of the plume stem is light grey. Eclogite contents on the two sides of the
620 plume core are labelled. Circles are contours of imposed potential temperature from 1375 °C
621 (outside, black) to 1625 °C (inside, white) in 25 °C increments. In each model, the center of the
622 plume at the base of the box is at $x = 3135$ km and $y = 1650$ km. The black arrow in the top-left
623 corner points northward.

624

625 **Fig. 5:** Temperature, melting, and net buoyancy of all cases (rows as annotated). Left column
626 shows perspective view from below of potential temperature (colors) with the 1550 and 1620°C
627 isosurfaces shown in translucent white and solid white, respectively. Grey and black isosurfaces
628 denote sites of minor and major magma generation, respectively. Middle and right columns show
629 cross-sections of net buoyancy (colored) perpendicular to plate motion. Net buoyancy is the sum
630 of thermal and compositional contributions, expressed as density deficit relative to the ambient
631 mantle at the reference potential temperature. Dashed-dotted lines mark the symmetry axis of the
632 model's initial and boundary conditions. Middle column (h-n) shows cross-sections through the
633 hottest part of the deep plume conduit and DEP. Right column shows cross-sections, slightly
634 further downstream, through the hottest part of the shallow plume conduit (i.e., close to the peak
635 hotspot melt production). Contours denote potential temperature in 50 °C increments with the
636 1500 °C isotherm dashed. Disk insets schematically show the initial distribution of eclogite,
637 similar to Fig. 4.

638

639 **Fig. 6:** Vertical cross-sections oriented perpendicular to plate motion of potential temperature
 640 (colors), initial eclogite content (white-to-black solid contours, see legend in upper right corner)
 641 and shape of the melting zone (dashed green contours for pyroxenite, dashed black for peridotite)
 642 for all cases. The initial eclogite content is the original content at the position of the material at
 643 the base of the model box, from where it has been advected (i.e., with the effects of eclogite
 644 melting removed). As shown by the solid contours running more-or-less vertically along the
 645 plume axis in the compositionally-zoned cases Z1-Z5, the two sides of the plume do not
 646 physically mix with each other. In cases S2 and Z3-Z5, temperatures across the melting zones
 647 are asymmetric in this cross-section, and the degrees of peridotite melting are higher (not shown)
 648 and the depth of the solidi (of both lithologies but of peridotitic lithologies in particular) are
 649 deeper on the hotter side of the hotspot melting zone. Pyroxenite melts to maximum degrees on
 650 both sides. Dashed-dotted lines mark the symmetry axis of the model's initial and boundary
 651 conditions. (*) For case S2, two different snapshots are shown, one of which (g) corresponds to
 652 the snapshot shown in Figure 8i, the other one of which (h) corresponds to that in Figure 8j.

653

654 **Fig. 7:** Plume upwelling rates, temperatures and initial eclogite contents (colors with black
 655 denoting 0%) for all cases (rows as annotated) in horizontal cross sections at 150 km, 250 km
 656 and 350 km depth (columns as annotated). Black-to-white contours denote mantle potential
 657 temperature in 10 °C increments between 1520 °C (white) and 1640 °C (black). Red contours
 658 denote plume upwelling rates on a log-scale (spaced by factor $\log_{10}(0.2)$). Disk insets (top)
 659 schematically show the initial distribution of eclogite, similar to Fig. 4. The black and red crosses
 660 (as well as the bull's eyes of the grey-to-black and of the red contours) mark the peak in plume
 661 temperature, and the focus of most vigorous upwelling, respectively. Whereas for cases S1 and
 662 Z1-Z2, the centers of these bull's eyes fall on top of each other, they are displaced from each
 663 other for cases S2 and Z3-Z5. Such a displacement identifies an asymmetry in temperature
 664 structure across the ascending plume. For reference, the deep plume stem at the bottom of the
 665 box (i.e., 660 km depth) is centered at $x = 3135$ km and $y = 1650$ km; plate motion is from right
 666 to left by rates of 80 km/Myr.

667

668 **Fig. 7:** continued.

669

670 **Fig. 8:** Geographical distribution of volcanism for all cases. Dark-grey contours show the flux of
 671 volcanism with solid contours at 0.1, 1, and 10 $\text{km}^3 \text{ km}^{-2} \text{ Myr}^{-1}$ from outside to inside. Colors
 672 display X_{PX} (note the difference in scales for panels (c-d) and (g) compared to the other panels).
 673 Insets zoom into the hotspot region (non-shaded and inside the black dashed line). The edge

674 lengths of the insets is 200 km, corresponding to a zoom factor of 2:1. White arrows mark the
 675 model's northern direction. For time-dependent case S2, only one snapshot is fully shown (b),
 676 but zooms into the hotspot region of three additional snapshots are also given (h-j). The snapshot
 677 shown in (i) corresponds to that in Figure 6g; the snapshot shown in (j) corresponds to that in
 678 Figure 6h. Averages of X_{PX} for each side of the hotspot are reported in Table 3.

679

680 **Fig. 9:** Synthetic seismic shear-wave velocities at 350 km depth (shades of grey). Shown are
 681 horizontal cross-sections through three-dimensional synthetic models computed from the
 682 predicted temperatures, densities, and eclogite contents of (a) a thermal plume model (Ballmer et
 683 al., 2011), (b-c) cases S1-S2, and (d-h) cases Z1-Z5. In interpolating the three-dimensional
 684 model to the cross-section shown, synthetic seismic velocities are averaged over a depth interval
 685 of 50 km. The dashed ellipse is analogous to that shown in Fig. 3e, and thus denotes the
 686 approximate size and location of the body of low seismic wave speeds imaged by joint seismic
 687 tomography (Cheng et al., this volume).

688

689 7. Appendix: Melting, density, and rheology parameterizations

690 7.1 Melting parameterization

691 The solidi versus depth functions, and the rate change in melt fraction per increment of
 692 pressure release of eclogite, pyroxenite and peridotite are parameterized using polynomial
 693 regressions to experimental data (Yasuda et al., 1994; Hirschmann, 2000; Pertermann and
 694 Hirschmann, 2003). We assume the rate of heat consumption by melting is proportional to the
 695 latent heat $L = 560$ kJ/kg and melting rate. However, the processes of eclogite melting and
 696 subsequent hybridization of the ambient peridotite to form pyroxenite together are assumed to
 697 neither consume nor release latent heat. As soon as the volume fraction of melt in a given
 698 lithology exceeds a critical porosity (i.e., $\varphi_C = 0.4\%$ in peridotite and $\varphi_{C,PYX} = 10\%$ in
 699 pyroxenite), magmas are instantaneously extracted and taken to feed volcanism (cf. McKenzie,
 700 1985; Schmeling, 2006); thereafter, the solid maintains residual porosities of $\varphi_R = 0.4\%$ and
 701 $\varphi_{R,PYX} = 5\%$. This treatment is equivalent to assuming that the timescale of melt extraction is
 702 much smaller than that of mantle flow (Kelemen et al., 1997). The porosities applied are
 703 bracketed by estimates (Yaxley and Green, 1998; Faul, 2001; Stracke et al., 2006).

704 Compared to that of dry peridotite, the melting temperature of hydrous peridotite is reduced
 705 with increasing water content in the liquid c_L (i.e., by $43c_L$ K/wt.-% (Katz et al., 2003)). The
 706 liquid water concentration decreases during melting as an inverse function of depletion (i.e.,
 707 extent of previous or ongoing melting) of hydrous peridotite F_{HP} :

$$708 \quad c_L = \frac{c}{D_{H_2O}} = \frac{c_0}{F_{HP} + D_{H_2O}(1 - F_{HP})} \quad (\text{Eq. 1})$$

709 for $F_{HP} < \varphi_C$, and

$$710 \quad c_L = \frac{c}{D_{H_2O}} = c_O \frac{\left(1 - \frac{F_{HP} - \varphi_C}{1 - \varphi_C}\right)^{\frac{1}{\varphi_C(1 - D_{H_2O}) + D_{H_2O}} - 1}}{\varphi_C + D_{H_2O}(1 - \varphi_C)} \quad (\text{Eq. 2})$$

711 for $F_{HP} \geq \varphi_C$ (Zou, 1998) with c the water content in the solid and D_{H_2O} the partitioning
712 coefficient of water.

713

714 7.2 Density parameterization

715 Mantle density varies as a function of temperature, composition and melt content:

$$716 \quad \rho = \rho_O - \alpha (T - T_O) + (\rho_M - \rho_O)\varphi + \Delta\rho_F(F_{DP}\Phi_{DP} + F_{HP}\Phi_{ECL}) + \Delta\rho_{ECL}\Phi_{ECL} \quad (\text{Eq. 3})$$

$$717 \quad \text{with} \quad \varphi = \varphi_{PYX}\Phi_{PYX} + \varphi_{DP}\Phi_{DP} + \varphi_{HP}\Phi_{HP} \quad (\text{Eq. 4})$$

718 and subscripts PYX, ECL, HP, and DP referring to the components pyroxenite, eclogite, hydrous
719 and dry peridotite, respectively; Φ_{XY} is volume fraction of a component; φ_{XY} is porosity in a
720 component; F_{XY} is depletion of a component; T is temperature; T_O is reference temperature; ρ is
721 density; ρ_O is reference density; α is thermal expansivity; φ is bulk porosity; ρ_M is density of
722 melt; $\Delta\rho_F$ is density change with depletion; and $\Delta\rho_{ECL}$ is excess density of eclogite. The densities
723 of both dry and hydrated peridotite decrease as depletion increases during progressive melting,
724 since heavy minerals and oxides are preferentially consumed during melting (Schutt and Leshner,
725 2006). In contrast, we assume the densities of eclogite and pyroxenite to be independent of
726 depletion (due to their relatively small volume fraction and uniform mineralogy, respectively).
727 $\Delta\rho_{ECL}$ was fixed at 220 kg/m³ in the depth range 300 to 410 km, and 110 kg/m³ elsewhere (Aoki
728 and Takahashi, 2004). We also ignore the effect of the refractory lithology on bulk density (i.e.,
729 by setting $\Delta\rho_{RL} \equiv 0$), assuming a negligible intrinsic negative density anomaly of this minor
730 component. As the volume fraction of the refractory component $\Phi_{RL} = \Phi_{ECL,SW} - \Phi_{ECL}$ (except for
731 where eclogite melting has taken place) with $\Phi_{ECL,SW}$ the initial volume fraction of eclogite on
732 the SW side of the plume stem (i.e., a constant for each calculation), $\Delta\rho_{RL}$ also largely trades off
733 with $\Delta\rho_{ECL}$.

734

735 7.3 Rheology parameterization

736 We apply a Newtonian rheology to model convection in the mantle. We neglect the stress-
737 dependence of mantle viscosity η , and focus on the effects of composition, temperature and melt.
738 While stress-dependent dislocation creep is relevant for plume-lithosphere interaction in the
739 asthenosphere (Asaadi et al., 2011), stress-independent diffusion creep is thought to be the
740 dominant mechanism of deformation in the lower upper mantle and at the depths of the DEP

741 (Karato and Wu, 1993). We chose an activation energy of $E^* = 300$ kJ/mol, which is appropriate
 742 for modeling diffusion creep (Karato and Wu, 1993; Hirth, 2002). Finally, we account for the
 743 effects of dehydration in olivine (Hirth and Kohlstedt, 1996) and melt retention on rheology
 744 (Kohlstedt and Zimmerman, 1996). Whereas melt retention lubricates the mantle, dehydration
 745 stiffening during progressive melting is thought to be dominant (Karato, 1986). We parameterize
 746 mantle rheology such, that hydrous peridotite stiffens by a factor of $\xi = 100$, as it dehydrates
 747 from $c = 100$ ppm to $c = c_{dry}$ (Hirth and Kohlstedt, 1996). Mantle rheology is instead taken to be
 748 insensitive to the abundance of olivine-free (eclogite, pyroxenite) lithologies, since deformation
 749 of a fine-scale (i.e., compared to the length-scale of convection) assemblage is predominantly
 750 compensated by the weakest lithology (i.e., peridotite) as long as it forms the matrix. Substituting
 751 Eq. 1 or Eq. 2 into Eq. 5 thus leaves with a rheology dependent on the depletion in hydrous
 752 peridotite F_{HP} and melt content ϕ , in addition to the dependence on temperature T and depth z :

$$753 \quad \eta = \eta_m \exp\left(\frac{E^* + \rho_m g z V^*}{RT} - \frac{E^*}{RT_m}\right) \frac{[(c - c_{dry}) \frac{\xi}{\xi - 1}]^{\Phi_{HP}}}{\exp(\zeta \phi)} \quad (\text{Eq. 5})$$

754 with η_m the reference mantle viscosity and all other parameters reported in Table 2. The effective
 755 mantle viscosity of $\eta_{eff} = 1.6 \cdot 10^{19}$ Pa·s defines the minimum viscosity of the asthenosphere in a
 756 mantle column well away from the hotspot, typically reached at ~ 160 km depth.

757

758 8. Acknowledgements

759 M.D.B. and G.I. were supported by NSF-grant EAR-1141938. Calculations were performed
 760 on NSF's TeraGrid (XSEDE) using allocation TG-EAR120012, as well as at the Hawaii Open
 761 Supercomputing Center. We thank associate editor Mike Poland and two anonymous reviewers
 762 for comments that helped to improve the manuscript.

763

764 9. References

- 765 Abouchami, W., Hofmann, A.W., Galer, S.J.G., Frey, F.A., Eisele, J., Feigenson, M., 2005. Lead
 766 isotopes reveal bilateral asymmetry and vertical continuity in the Hawaiian mantle plume.
 767 Nature. 434, 851-856.
- 768 Aoki, I., Takahashi, E., 2004. Density of MORB eclogite in the upper mantle. Phys. Earth Planet.
 769 Inter. 143, 129-143.
- 770 Asaadi, N., Ribe, N.M., Sobouti, F., 2011. Inferring nonlinear mantle rheology from the shape of
 771 the Hawaiian swell. Nature. 473, 501-504.
- 772 Ballmer, M.D., Ito, G., van Hunen, J., Tackley, P.J., 2010. Small-scale sublithospheric
 773 convection reconciles geochemistry and geochronology of 'Superplume' volcanism in the
 774 western and south Pacific. Earth Planet. Sci. Lett. 290, 224-232.

- 775 Ballmer, M.D., Ito, G., van Hunen, J., Tackley, P.J., 2011. Spatial and temporal variability in
776 Hawaiian hotspot volcanism induced by small-scale convection. *Nature Geoscience*. 4,
777 457-460.
- 778 Ballmer, M.D., Ito, G., Wolfe, C.J., Solomon, S.C., 2013. Double layering of a thermochemical
779 plume in the upper mantle beneath Hawaii. *Earth Planet. Sci. Lett.*, in press.
- 780 Ballmer, M.D., van Hunen, J., Ito, G., Tackley, P.J., Bianco, T.A., 2007. Non-hotspot volcano
781 chains originating from small-scale sublithospheric convection. *Geophys. Res. Lett.* 34.
- 782 Boyet, M., Carlson, R.W., 2005. Nd-142 evidence for early (> 4.53 Ga) global differentiation of
783 the silicate Earth. *Science*. 309, 576-581.
- 784 Burke, K., Torsvik, T.H., 2004. Derivation of Large Igneous Provinces of the past 200 million
785 years from long-term heterogeneities in the deep mantle. *Earth Planet. Sci. Lett.* 227,
786 531-538.
- 787 Castillo, P.R., Natland, J.H., Niu, Y.L., Lonsdale, P.F., 1998. Sr, Nd and Pb isotopic variation
788 along the Pacific-Antarctic rise crest, 53-57 degrees S: Implications for the composition
789 and dynamics of the South Pacific upper mantle. *Earth Planet. Sci. Lett.* 154, 109-125.
- 790 Chauvel, C., Maury, R.C., Blais, S., Lewin, E., Guillou, H., Guille, G., Rossi, P., Gutscher, M.-
791 A., 2012. The size of plume heterogeneities constrained by Marquesas isotopic stripes.
792 *Geochemistry Geophysics Geosystems*. 13, Q07005.
- 793 Cheng, C., Allen, R.M., Porritt, R.W., Ballmer, M.D., Seismic constraints on a double-layered
794 asymmetric whole-mantle plume beneath Hawaii, in: R. Carey, D. Weis, M. Poland,
795 (Eds), *Hawaiian Volcanism: From Source to Surface*, AGU Monograph, this volume.
- 796 Crosby, A.G., McKenzie, D., 2009. An analysis of young ocean depth, gravity and global
797 residual topography. *Geophys. J. Int.* 178, 1198-1219.
- 798 Davaille, A., 1999. Simultaneous generation of hotspots and superswells by convection in a
799 heterogeneous planetary mantle. *Nature*. 402, 756-760.
- 800 Dupre, B., Allegre, C.J., 1983. Pb-Sr variation in Indian Ocean basalts and mixing phenomena.
801 *Nature*. 303, 142-146.
- 802 Farnetani, C.G., Hofmann, A.W., 2009. Dynamics and internal structure of a lower mantle plume
803 conduit. *Earth Planet. Sci. Lett.* 282, 314-322.
- 804 Farnetani, C.G., Hofmann, A.W., 2010. Dynamics and internal structure of the Hawaiian plume.
805 *Earth Planet. Sci. Lett.* 295, 231-240.
- 806 Farnetani, C.G., Hofmann, A.W., Class, C., 2012. How double volcanic chains sample
807 geochemical anomalies from the lowermost mantle. *Earth Planet. Sci. Lett.* 359, 240-247.
- 808 Farnetani, C.G., Samuel, H., 2005. Beyond the thermal plume paradigm. *Geophys. Res. Lett.* 32.
- 809 Faul, U., 2001. Melt retention and segregation beneath mid-ocean ridges. *Nature*. 410, 920-923.
- 810 Faul, U.H., Jackson, I., 2005. The seismological signature of temperature and grain size
811 variations in the upper mantle *Earth Planet. Sci. Lett.* 234, 119-134.
- 812 Frey, F.A., Rhodes, J.M., 1993. Intershield geochemical differences among Hawaiian volcanoes
813 - implications for source compositions, melting process and magma ascent paths. *Phil.*
814 *Trans. R. Soc. Lond. A*. 342, 121-136.
- 815 Greene, A.R., Garcia, M.O., Weis, D., Ito, G., Kuga, M., Robinson, J., Yamasaki, S., 2010. Low-
816 productivity Hawaiian volcanism between Kaua'i and O'ahu. *Geochem. Geophys.*
817 *Geosyst.* 11, Q0AC08.
- 818 Griffiths, R.W., Campbell, I.H., 1990. Stirring and Structure In Mantle Starting Plumes. *Earth*
819 *Planet. Sci. Lett.* 99, 66-78.

- 820 Hauri, E.H., 1996. Major element variability in the Hawaiian mantle plume. *Nature*. 382, 415-
821 419.
- 822 Herzberg, C., 2011. Identification of source lithology in the Hawaiian and Canary Islands:
823 implications for origins. *J. Petrol.* 52, 113-146.
- 824 Herzberg, C., Asimow, P.D., Arndt, N., Niu, Y.L., Leshner, C.M., Fitton, J.G., Cheadle, M.J.,
825 Saunders, A.D., 2007. Temperatures in ambient mantle and plumes: constraints from
826 basalts, picrites, and komatiites. *Geochem. Geophys. Geosyst.* 8, 34.
- 827 Hirschmann, M.M., 2000. Mantle solidus: experimental constraints and the effects of peridotite
828 composition. *Geochem. Geophys. Geosyst.* 1.
- 829 Hirschmann, M.M., Stolper, E.M., 1996. A possible role for garnet pyroxenite in the origin of the
830 "garnet signature" in MORB. *Contrib. Mineral. Petrol.* 124, 185-208.
- 831 Hirth, G., 2002. Laboratory constraints on the rheology of the upper mantle. *Plastic Deformation
832 of Minerals and Rocks.* 51, 97-120.
- 833 Hirth, G., Kohlstedt, D.L., 1996. Water in the oceanic upper mantle - Implications for rheology,
834 melt extraction and the evolution of the lithosphere. *Earth Planet. Sci. Lett.* 144, 93-108.
- 835 Hirth, G., Kohlstedt, D.L., Rheology of the upper mantle and mantle wedge: A view from the
836 experimentalists, in: J. Eiler, (Ed), *Inside the subduction factory*, AGU, Washington, D.
837 C., 2003, pp. 83-105.
- 838 Huang, S., Hall, P.S., Jackson, M.G., 2011. Geochemical zoning of volcanic chains associated
839 with Pacific hotspots. *Nature Geoscience.* 4, 874-878.
- 840 Huang, S., Humayun, M., Frey, F.A., 2007. Iron/manganese ratio and manganese content in
841 shield lavas from Ko'olau Volcano, Hawai'i. *Geochimica et Cosmochimica Acta.* 71,
842 4557-4569.
- 843 Huang, S.C., Frey, F.A., 2005. Recycled oceanic crust in the Hawaiian Plume: evidence from
844 temporal geochemical variations within the Koolau Shield. *Contributions to Mineralogy
845 and Petrology.* 149, 556-575.
- 846 Ishii, M., Tromp, J., 1999. Normal-mode and free-air gravity constraints on lateral variations in
847 velocity and density of Earth's mantle. *Science.* 285, 1231-1235.
- 848 Jackson, E.D., Silver, E.A., Dalrymple, G.B., 1972. Hawaiian-Emperor chain and its relation to
849 Cenozoic circumpacific tectonics. *Geol. Soc. Amer. Bull.* 83, 601-618.
- 850 Jackson, M.G., Weis, D., Huang, S., 2012. Major element variations in Hawaiian shield lavas:
851 Source features and perspectives from global ocean island basalt (OIB) systematics.
852 *Geochem. Geophys. Geosyst.*, Q09009.
- 853 Karato, S., 1986. Does partial melting reduce the creep strength of the upper mantle. *Nature.* 319,
854 309-310.
- 855 Karato, S., Wu, P., 1993. Rheology of the upper mantle - a synthesis. *Science.* 260, 771-778.
- 856 Katz, R.F., Rudge, J.F., 2011. The energetics of melting fertile heterogeneities within the
857 depleted mantle. *Geochemistry Geophysics Geosystems.* 12.
- 858 Katz, R.F., Spiegelman, M., Langmuir, C.H., 2003. A new parameterization of hydrous mantle
859 melting. *Geochem. Geophys. Geosyst.* 4, 1073.
- 860 Kelemen, P.B., Hirth, G., Shimizu, N., Spiegelman, M., Dick, H.J.B., 1997. A Review Of Melt
861 Migration Processes In the Adiabatically Upwelling Mantle Beneath Oceanic Spreading
862 Ridges. *Philosophical Transactions Of the Royal Society Of London Series a
863 Mathematicalphysical and Engineering Sciences.* 355, 283-318.
- 864 Kohlstedt, D.L., Zimmerman, M.E., 1996. Rheology of partially molten mantle rocks. *Ann. Rev.
865 Earth Planet. Sci.* 24, 41-62.

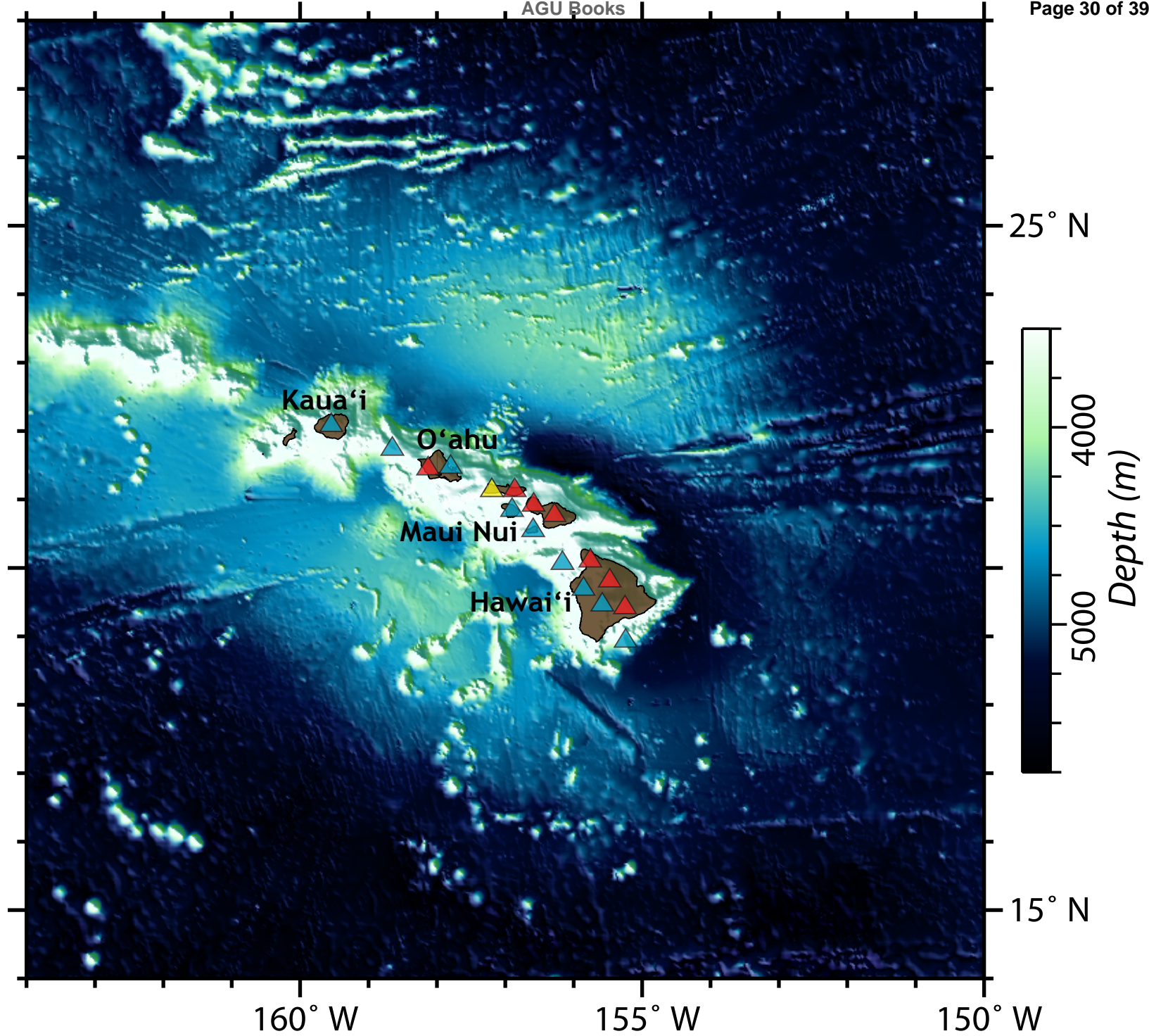
- 866 Konter, J.G., Hanan, B.B., Blichert-Toft, J., Koppers, A.A.P., Plank, T., Staudigel, H., 2008. One
867 hundred million years of mantle geochemical history suggest the retiring of mantle
868 plumes is premature. *Earth Planet. Sci. Lett.* 275, 285-295.
- 869 Kumagai, I., Davaille, A., Kurita, K., Stutzmann, E., 2008. Mantle plumes: Thin, fat, successful,
870 or failing? Constraints to explain hot spot volcanism through time and space. *Geophys.*
871 *Res. Lett.* 35, L16301.
- 872 Kurz, M.D., Kenna, T.C., Lassiter, J.C., DePaolo, D.J., 1996. Helium isotopic evolution of
873 Mauna Kea Volcano: First results from the 1-km drill core. *Journal of Geophysical*
874 *Research-Solid Earth.* 101, 11781-11791.
- 875 Labrosse, S., Hernlund, J.W., Coltice, N., 2007. A crystallizing dense magma ocean at the base
876 of the Earth's mantle. *Nature.* 450, 866-869.
- 877 Lin, S.C., van Keken, P.E., 2005. Multiple volcanic episodes of flood basalts caused by
878 thermochemical mantle plumes. *Nature.* 436, 250-252.
- 879 Mallik, A., Dasgupta, R., 2012. Reaction between MORB-eclogite derived melts and fertile
880 peridotite and generation of ocean island basalts. *Earth Planet. Sci. Lett.* 329, 97-108.
- 881 Masters, G., Laske, G., Bolton, H., Dziewonski, A., The relative behavior of shear velocity, bulk
882 sound speed, and compressional velocity in the mantle: Implications for chemical and
883 thermal structure., in: S. Karato, A.M. Forte, R.C. Liebermann, G. Masters, L. Stixrude,
884 (Eds), *Geophysical Monograph on Mineral Physics and Seismic Tomography from the*
885 *atomic to the global scale*, American Geophysical Union, 2000, pp. 63-87.
- 886 McKenzie, D., 1985. The Extraction Of Magma From the Crust and Mantle. *Earth Planet. Sci.*
887 *Lett.* 74, 81-91.
- 888 Moresi, L., Zhong, S., Gurnis, M., 1996. The accuracy of finite element solutions of Stokes' flow
889 with strongly varying viscosity. *Phys. Earth Planet. Int.* 97, 83-94.
- 890 Morgan, W.J., 1972. Plate motions and deep mantle convection. *Geol. Soc. Am. Memoir.* 132, 7-
891 22.
- 892 Mosca, I., Cobden, L., Deuss, A., Ritsema, J., Trampert, J., 2012. Seismic and mineralogical
893 structures of the lower mantle from probabilistic tomography. *J. Geophys. Res.* 117,
894 B06304.
- 895 Payne, J.A., Jackson, M.G., Hall, P.S., 2013. Parallel volcano trends and geochemical
896 asymmetry of the Society Islands hotspot track. *Geology.* 41, 19-22.
- 897 Pertermann, M., Hirschmann, M.M., 2003. Partial melting experiments on a MORB-like
898 pyroxenite between 2 and 3 GPa: Constraints on the presence of pyroxenite in basalt
899 source regions from solidus location and melting rate. *J. Geophys. Res.* 108, 2125.
- 900 Phipps Morgan, J., 2001. Thermodynamics of pressure release melting of a veined plum pudding
901 mantle. *Geochem. Geophys. Geosyst.* 2, 2000GC000049.
- 902 Pietruszka, A.J., Norman, M.D., Garcia, M.O., Marske, J.P., Burns, D.H., 2013. Chemical
903 heterogeneity in the Hawaiian mantle plume from the alteration and dehydration of
904 recycled oceanic crust. *Earth Planet. Sci. Lett.* 361, 298-309.
- 905 Putirka, K., Ryerson, F.J., Perfit, M., Ridley, W.I., 2011. Mineralogy and Composition of the
906 Oceanic Mantle. *Journal of Petrology.* 52, 279-313.
- 907 Ribe, N.M., Christensen, U.R., 1994. Three-dimensional modeling of plume-lithosphere
908 interaction. *J. Geophys. Res.* 99, 669-682.
- 909 Ribe, N.M., Christensen, U.R., 1999. The dynamical origin of Hawaiian volcanism. *Earth Planet.*
910 *Sci. Lett.* 171, 517-531.

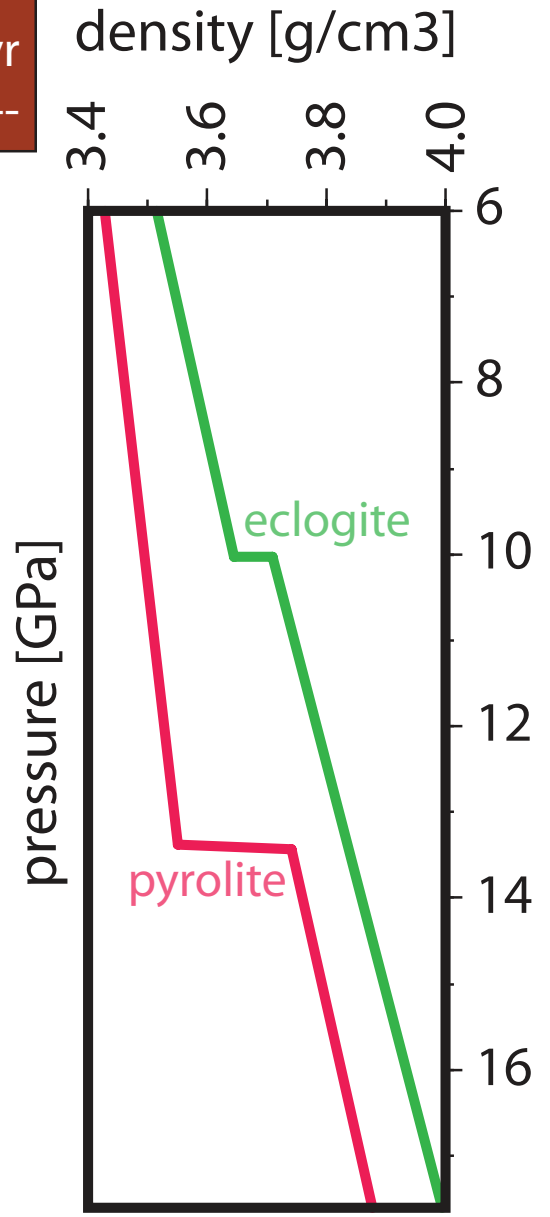
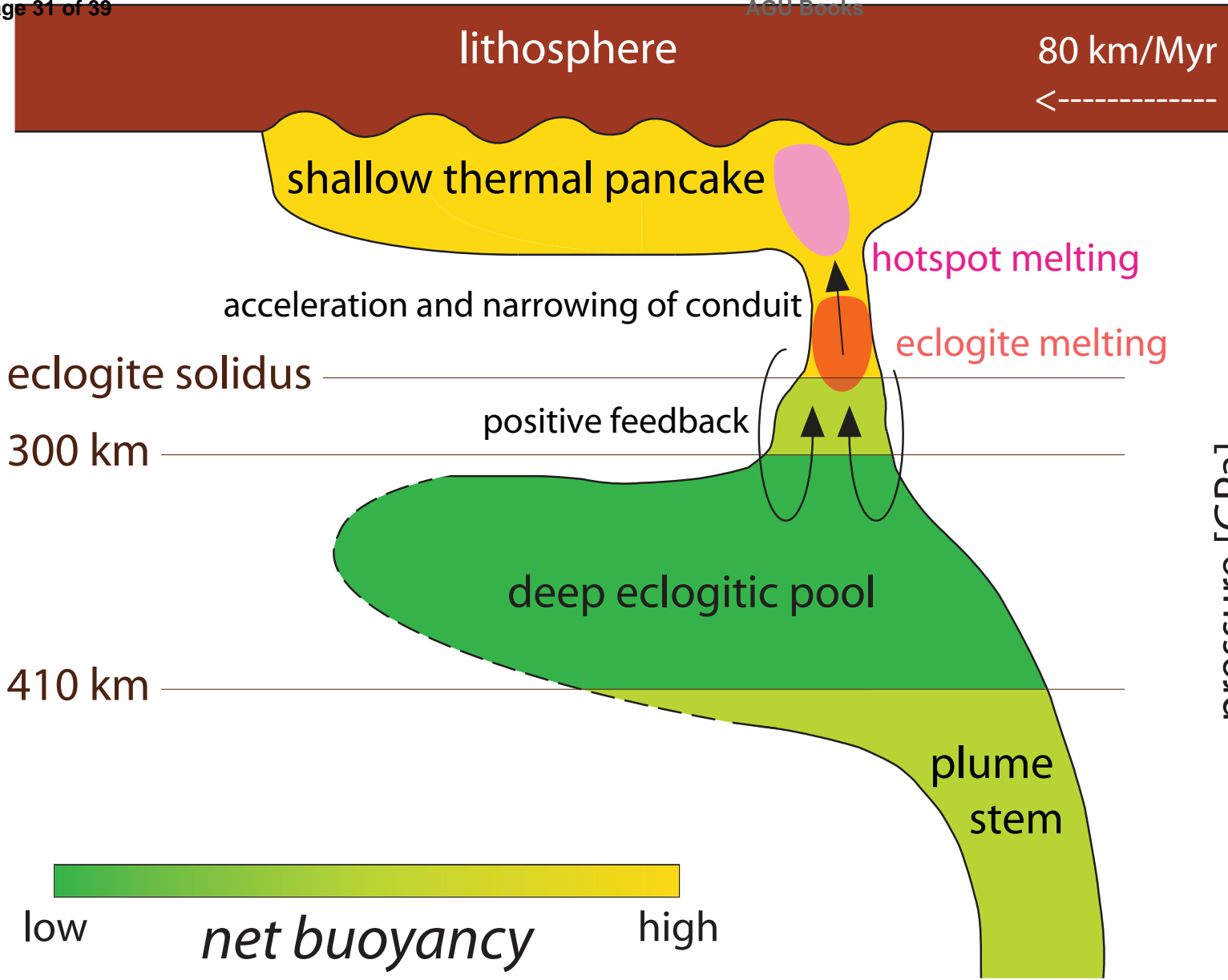
- 911 Robinson, J.E., Eakins, B.W., 2006. Calculated volumes of individual shield volcanoes at the
912 young end of the Hawaiian Ridge. *J. Volcanology Geothermal Res.* 151, 309-317.
- 913 Rychert, C.A., Laske, G., Harmon, N., Shearer, P.M., 2013. Seismic imaging of melt in a
914 displaced Hawaiian plume. *Nature Geosci.* 6, 657-660.
- 915 Schmeling, H., 2006. A model of episodic melt extraction for plumes. *J. Geophys. Res.* 111,
916 B03202, doi:10.1029/2004JB003423.
- 917 Schutt, D.L., Leshner, C.E., 2006. Effects of melt depletion on the density and seismic velocity of
918 garnet and spinel lherzolite. *J. Geophys. Res.* 111, B05401.
- 919 Sinton, J., Eason, D.E., Tardona, M., Pyle, D.G., van der Zander, I., Guillou, H., Flinders, A.,
920 Clague, D.A., Mahoney, J.J., in review. Ka'ena Volcano – a precursor volcano of the
921 island of O'ahu, Hawai'i.
- 922 Sleep, N.H., 1990. Hotspots and mantle plumes - some phenomenology. *J. Geophys. Res.* 95,
923 6715-6736.
- 924 Sobolev, A.V., Hofmann, A.W., Kuzmin, D.V., Yaxley, G.M., Arndt, N.T., Chung, S.L.,
925 Danyushevsky, L.V., Elliott, T., Frey, F.A., Garcia, M.O., Gurenko, A.A., Kamenetsky,
926 V.S., Kerr, A.C., Krivolutskaya, N.A., Matvienkov, V.V., Nikogosian, I.K., Rocholl, A.,
927 Sigurdsson, I.A., Sushchevskaya, N.M., Teklay, M., 2007. The amount of recycled crust
928 in sources of mantle-derived melts. *Science.* 316, 412-417.
- 929 Sobolev, A.V., Hofmann, A.W., Sobolev, S.V., Nikogosian, I.K., 2005. An olivine-free mantle
930 source of Hawaiian shield basalts. *Nature.* 434, 590-597.
- 931 Sobolev, S.V., Sobolev, A.V., Kuzmin, D.V., Krivolutskaya, N.A., Petrunin, A.G., Arndt, N.T.,
932 Radko, V.A., Vasiliev, Y.R., 2011. Linking mantle plumes, large igneous provinces and
933 environmental catastrophes. *Nature.* 477, 312-316.
- 934 Steinberger, B., Antretter, M., 2006. Conduit diameter and buoyant rising speed of mantle
935 plumes: Implications for the motion of hot spots and shape of plume conduits.
936 *Geochemistry Geophysics Geosystems.* 7, Q11018.
- 937 Steinberger, B., Torsvik, T.H., 2012. A geodynamic model of plumes from the margins of Large
938 Low Shear Velocity Provinces. *Geochemistry Geophysics Geosystems.* 13, Q01w09.
- 939 Stracke, A., Bourdon, B., McKenzie, D., 2006. Melt extraction in the Earth's mantle: Constraints
940 from U-Th-Pa-Ra studies in oceanic basalts. *Earth Planet. Sci. Lett.* 244, 97-112.
- 941 Stracke, A., Snow, J.E., Hellebrand, E., von der Handt, A., Bourdon, B., Birbaum, K., Günther,
942 D., 2011. Abyssal peridotite Hf isotopes identify extreme mantle depletion. *Earth Planet.*
943 *Sci. Lett.* 308, 359-368.
- 944 Torsvik, T.H., Burke, K., Steinberger, B., Webb, S.J., Ashwal, L.D., 2010. Diamonds sampled
945 by plumes from the core-mantle boundary. *Nature.* 466, 352-U100.
- 946 Torsvik, T.H., Smethurst, M.A., Burke, K., Steinberger, B., 2006. Large igneous provinces
947 generated from the margins of the large low-velocity provinces in the deep mantle.
948 *Geophys. J. Int.*, doi:10.1111/j.1365-1246X.2006.03158.x.
- 949 van Ark, E., Lin, J., 2004. Time variation in igneous volume flux of the Hawaii-Emperor hot
950 spot seamount chain. *J. Geophys. Res.* 109, B11401
- 951 Vidal, V., Bonneville, A., 2004. Variations of the Hawaiian hot spot activity revealed by
952 variations in the magma production rate. *J. Geophys. Res.* 109, B03104.
- 953 Weis, D., Garcia, M.O., Rhodes, J.M., Jellinek, M., Scoates, J.S., 2011. Role of the deep mantle
954 in generating the compositional asymmetry of the Hawaiian mantle plume. *Nature*
955 *Geosci.* 4, 831-838.

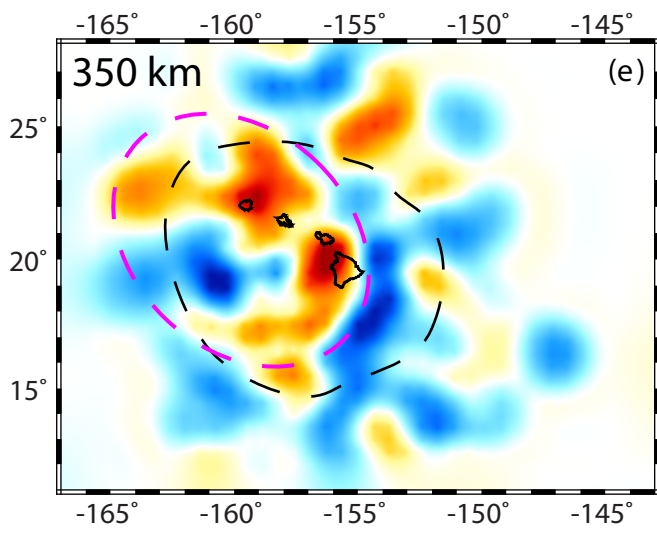
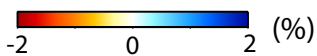
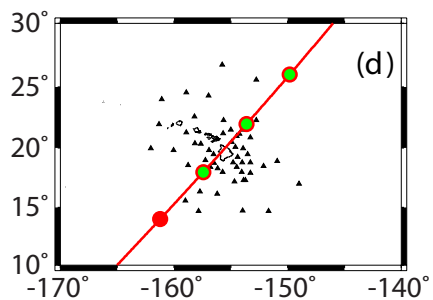
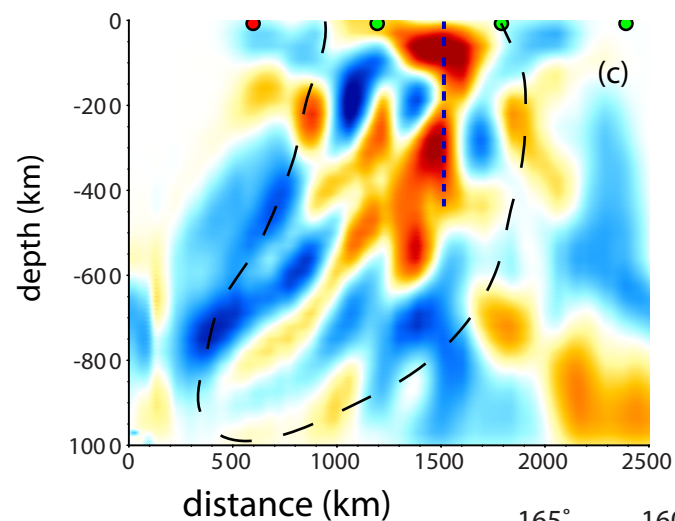
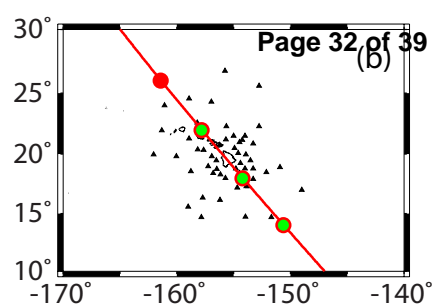
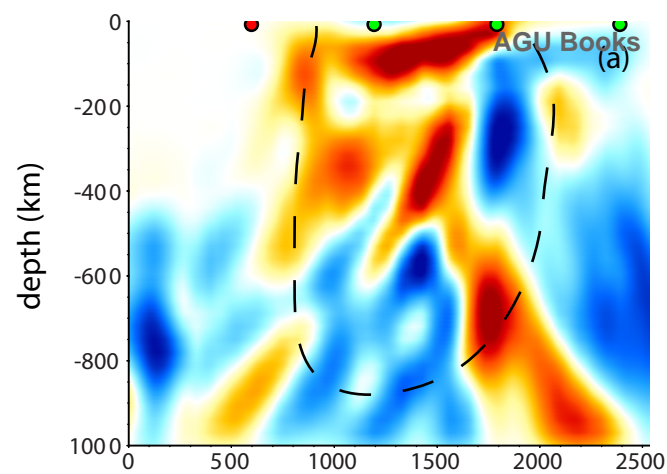
- 956 Wen, L., 2006. A compositional anomaly at the Earth's core-mantle boundary as an anchor to the
957 relatively slowly moving surface hotspots and as source to the DUPAL anomaly. *Earth*
958 *Planet. Sci. Lett.* 246, 138-148.
- 959 Wen, L.X., Silver, P., James, D., Kuehnel, R., 2001. Seismic evidence for a thermo-chemical
960 boundary at the base of the Earth's mantle. *Earth Planet. Sci. Lett.* 189, 141-153.
- 961 Wessel, P., 1993. Observational constraints on models of the Hawaiian hot-spot swell. *J.*
962 *Geophys. Res.* 98, 16095-16104.
- 963 Wolfe, C.J., Solomon, S.C., Laske, G., Collins, J.A., Detrick, R.S., Orcutt, J.A., Bercovici, D.,
964 Hauri, E.H., 2009. Mantle Shear-Wave Velocity Structure Beneath the Hawaiian Hot
965 Spot. *Science.* 326, 1388-1390.
- 966 Wolfe, C.J., Solomon, S.C., Laske, G., Collins, J.A., Detrick, R.S., Orcutt, J.A., Bercovici, D.,
967 Hauri, E.H., 2011. Mantle P-wave Velocity Structure beneath the Hawaiian Hotspot.
968 *Earth Plan. Sci. Lett.*, doi:10.1016/j.epsl.2011.1001.1004.
- 969 Workman, R.K., Hart, S.R., Jackson, M., Regelous, M., Farley, K.A., Blusztajn, J., Kurz, M.,
970 Staudigel, H., 2004. Recycled metasomatized lithosphere as the origin of the enriched
971 mantle II (EM2) end-member: Evidence from the Samoan volcanic chain. *Geochemistry*
972 *Geophysics Geosystems.* 5.
- 973 Xu, G., Huang, S., Frey, F.A., Blichert-Toft, J., Abouchami, W., Clague, D.A., Cousens, B.,
974 Moore, J.G., Beeson, M.H., in press. The Distribution of Geochemical Heterogeneities in
975 the Source of Hawaiian Shield Lavas as Revealed by a Transect Across the Strike of the
976 Loa and Kea Spatial Trends: East Molokai to West Molokai to Penguin Bank. *Geochem.*
977 *Cosmochem. Acta.*
- 978 Xu, W., Lithgow-Bertelloni, C., Stixrude, L., Ritsema, J., 2008. The effect of bulk composition
979 and temperature on mantle seismic structure. *Earth Planet. Sci. Lett.* 275, 70-79.
- 980 Yasuda, A., Fujii, T., Kurita, K., 1994. Melting phase-relations of an anhydrous midocean ridge
981 basalt from 3 to 20 GPa - implications for the behavior of subducted oceanic-crust in the
982 mantle. *J. Geophys. Res.* 99, 9401-9414.
- 983 Yaxley, G.M., Green, D.H., 1998. Reactions between eclogite and peridotite: Mantle
984 refertilisation by subduction of oceanic crust. *Schweizerische Mineralogische und*
985 *Petrographische Mitteilungen.* 78, 243-255.
- 986 Zou, H.B., 1998. Trace element fractionation during modal and nonmodal dynamic melting and
987 open-system melting: A mathematical treatment. *Geochem. Cosmochem. Acta.* 62, 1937-
988 1945.

989

990

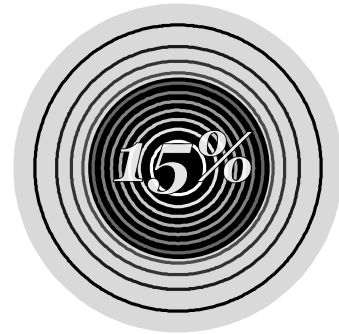
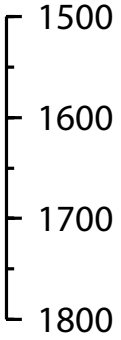
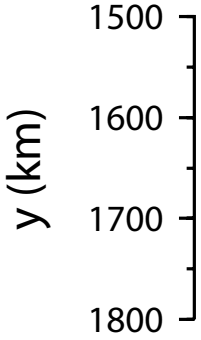






case S1 AGU Books

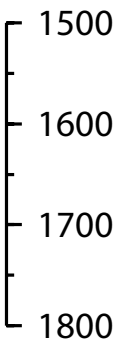
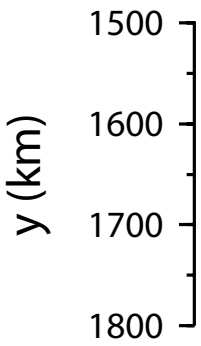
case S2



case Z1

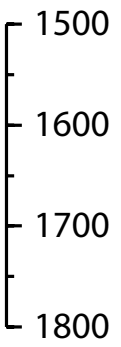
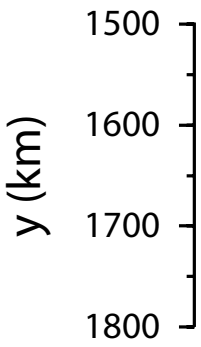
case Z2

case Z3



case Z4

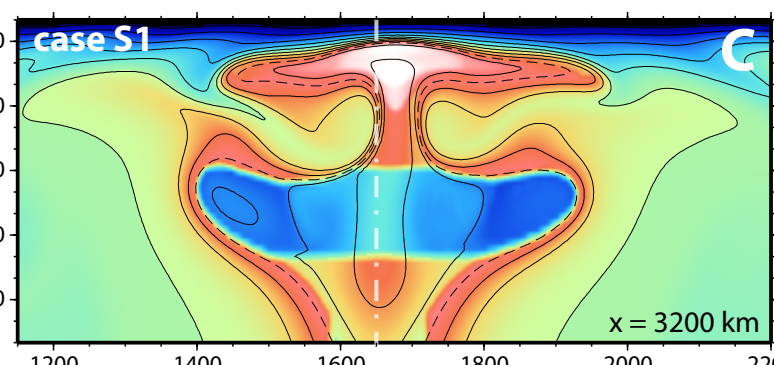
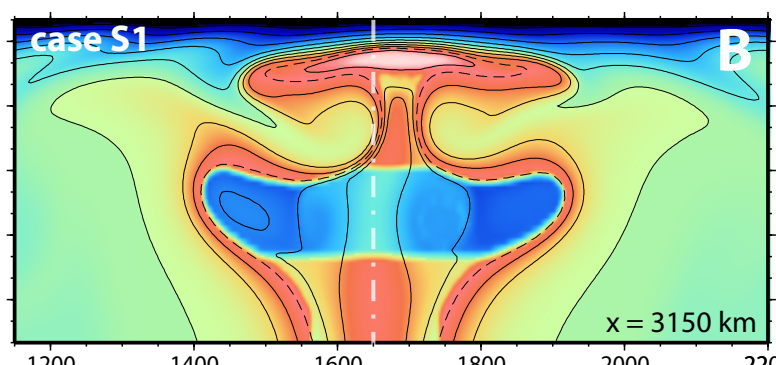
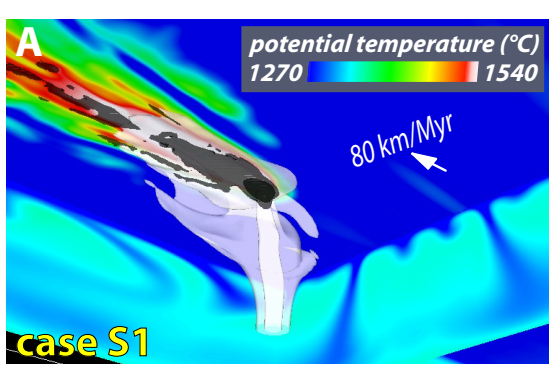
case Z5



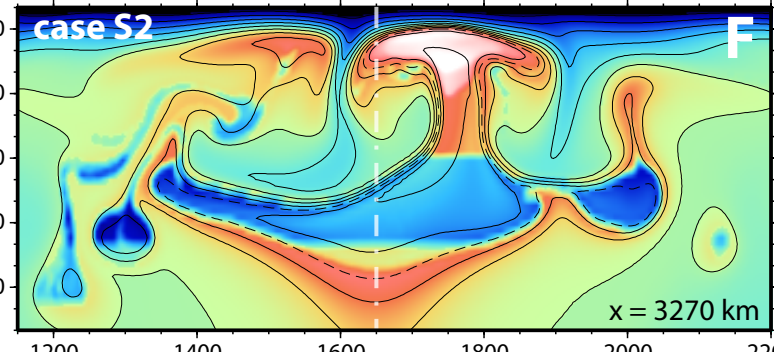
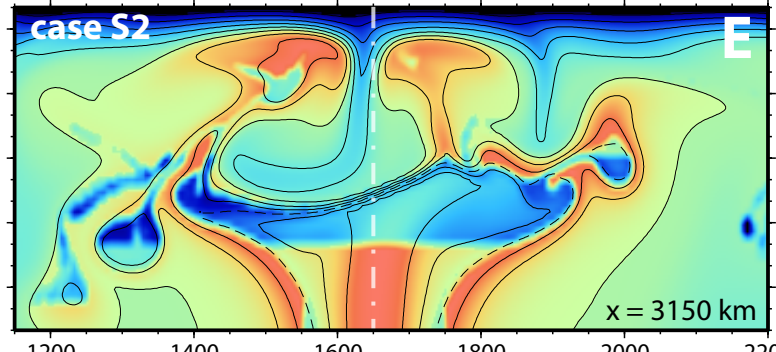
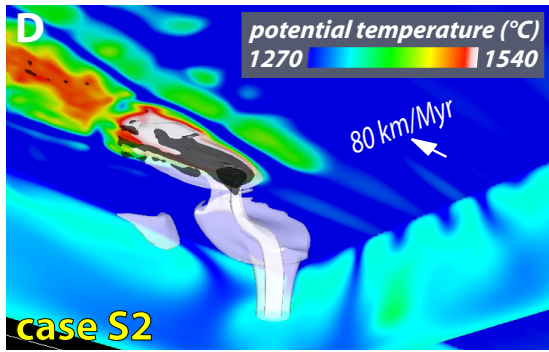
NE AGU Books SW

NE SW

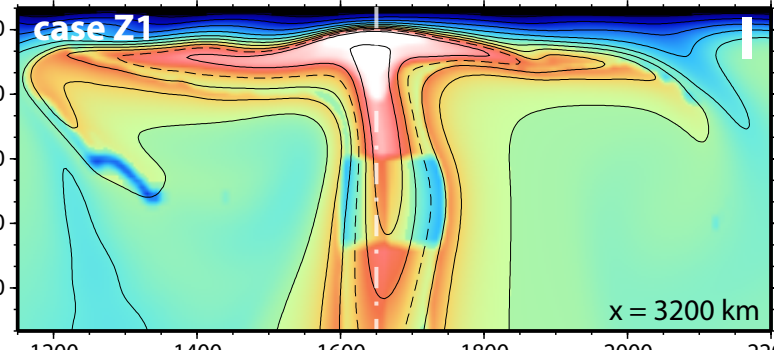
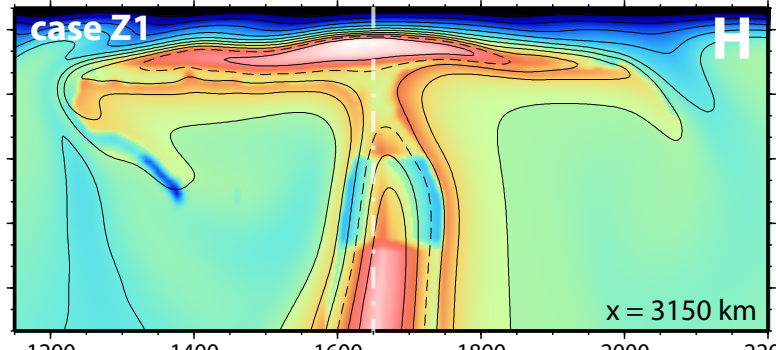
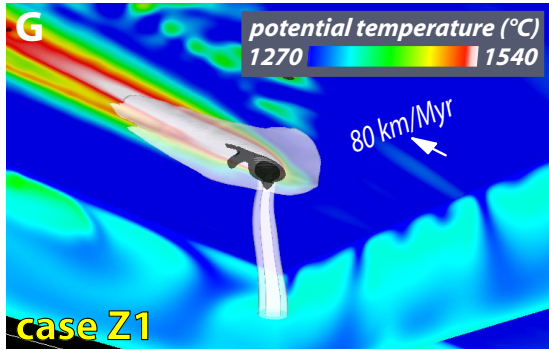
15%



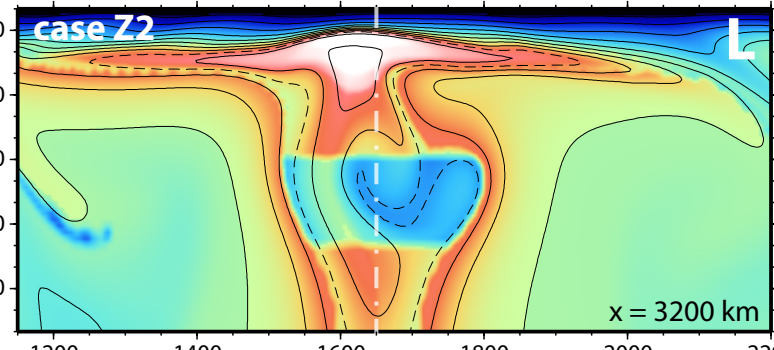
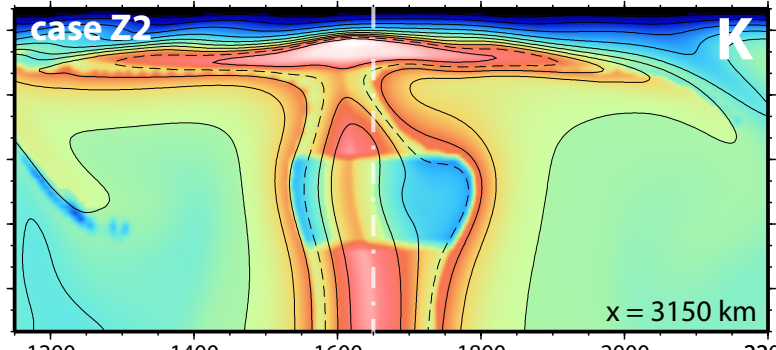
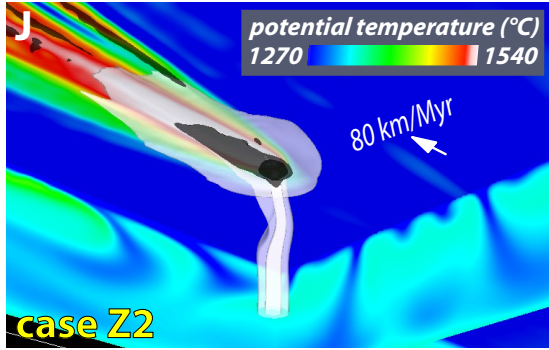
15%



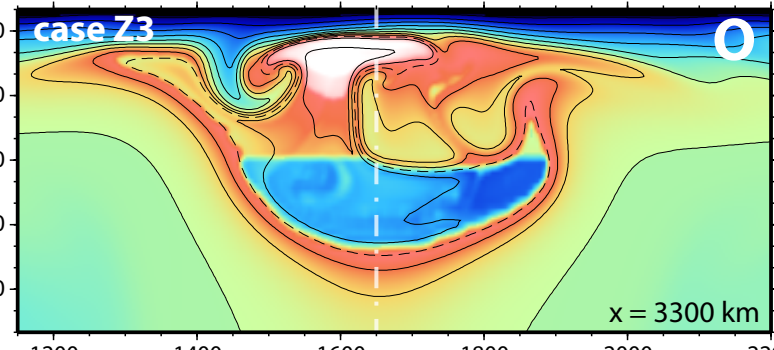
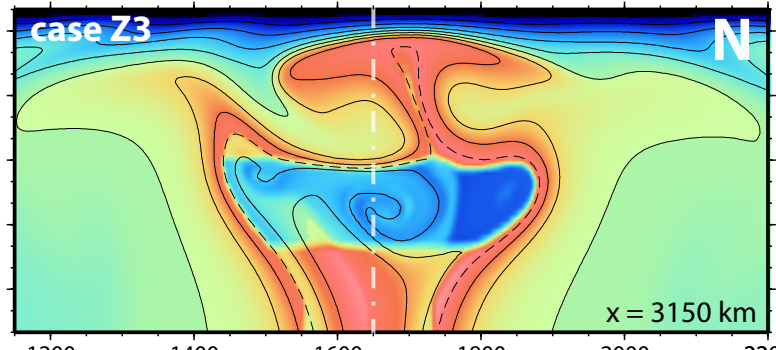
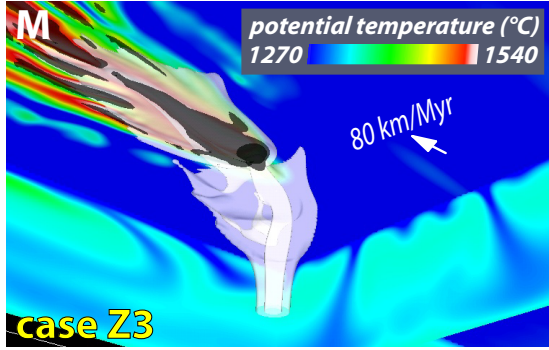
10%
8%



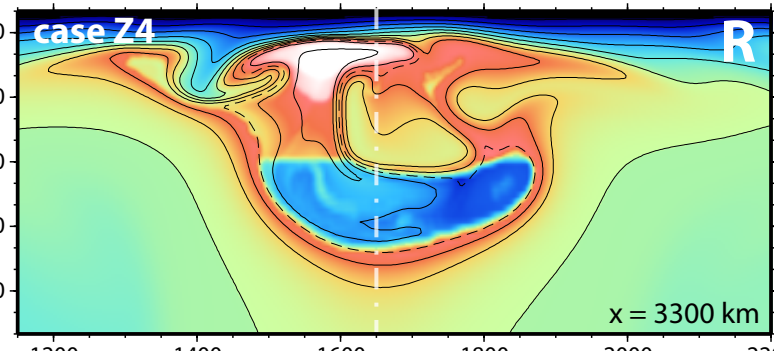
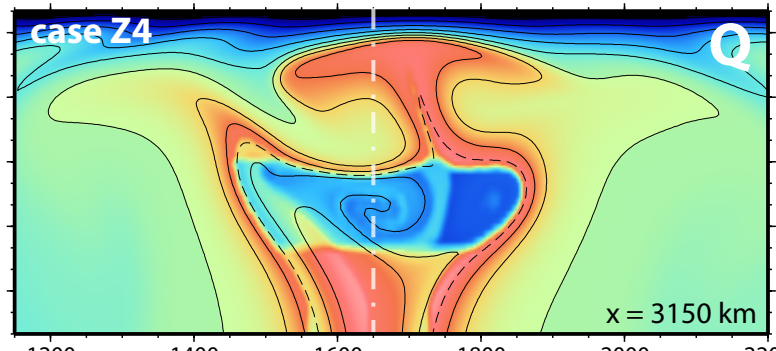
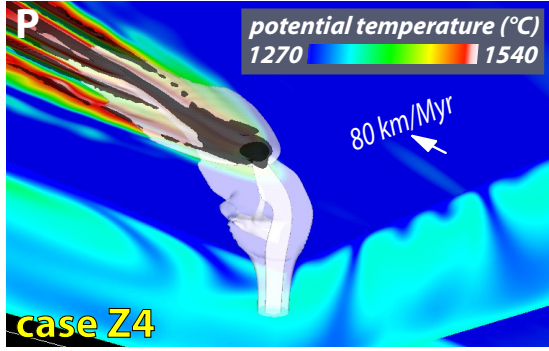
12%
10%



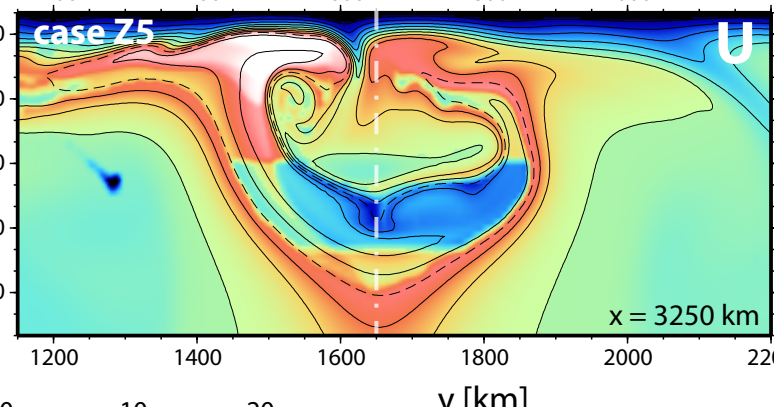
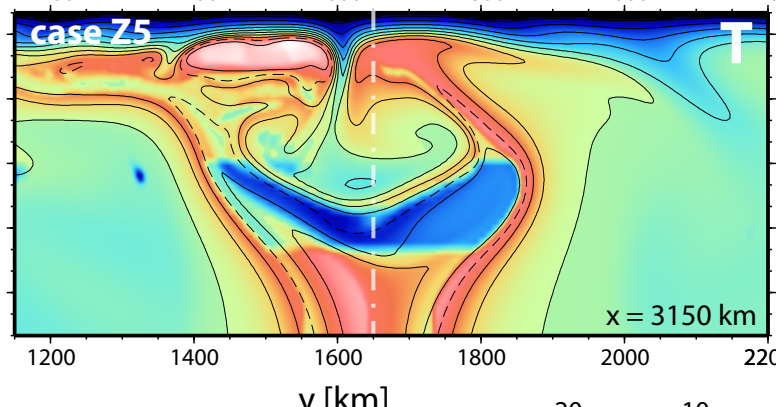
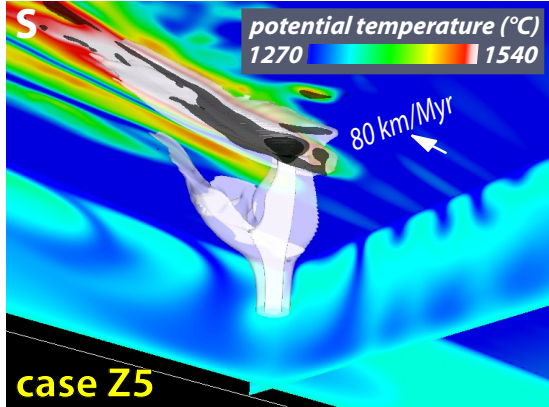
15%
12%



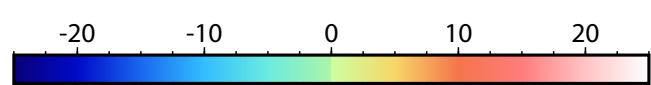
15%
11%



16%
10%

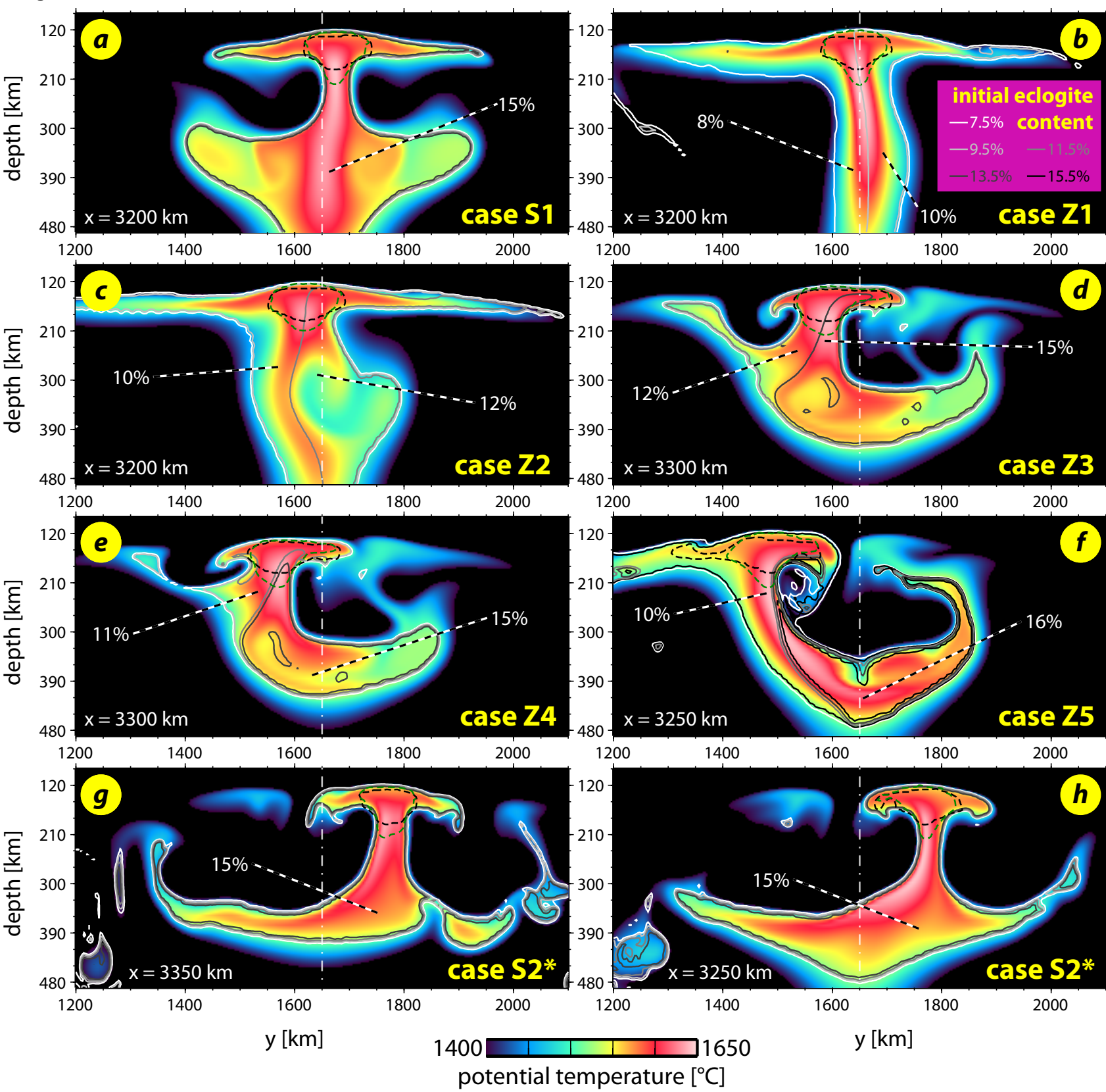


y [km]



buoyancy [kg/m³]

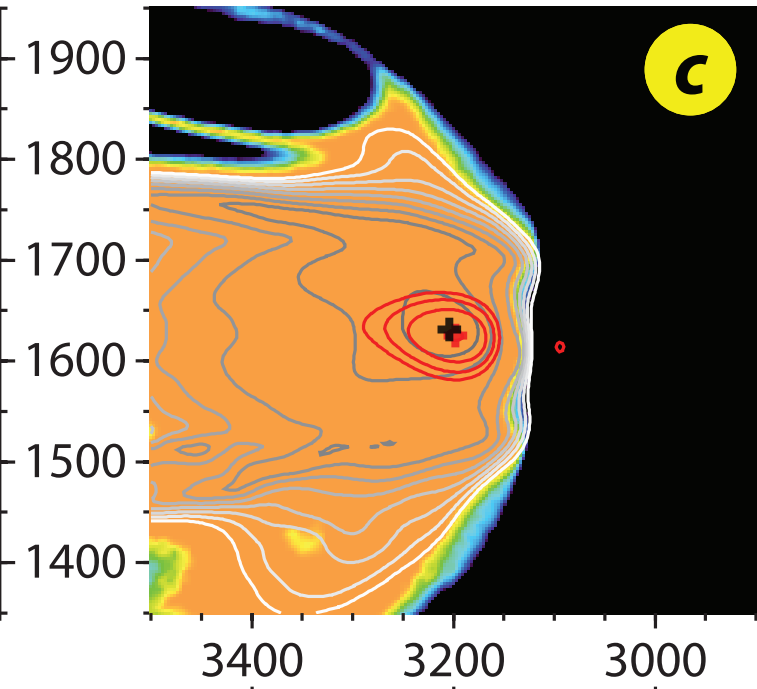
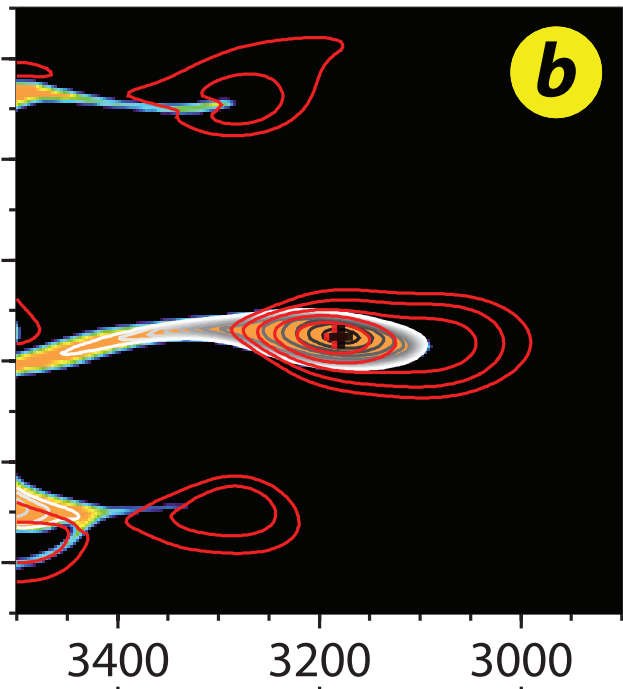
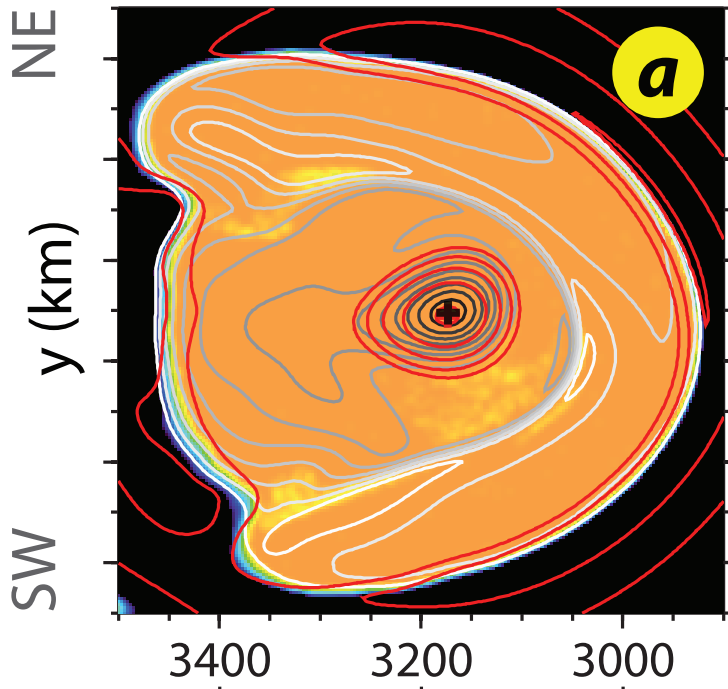
depth [km]



350 km

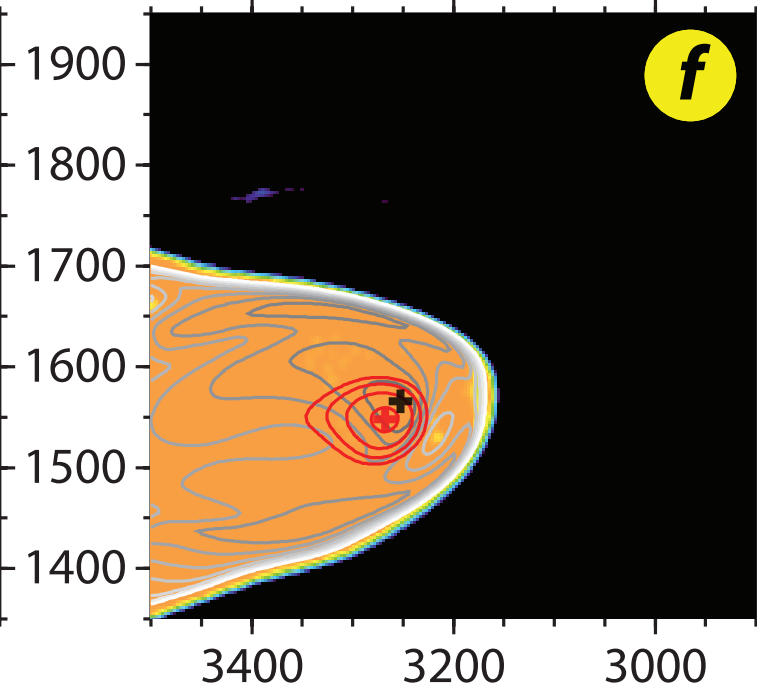
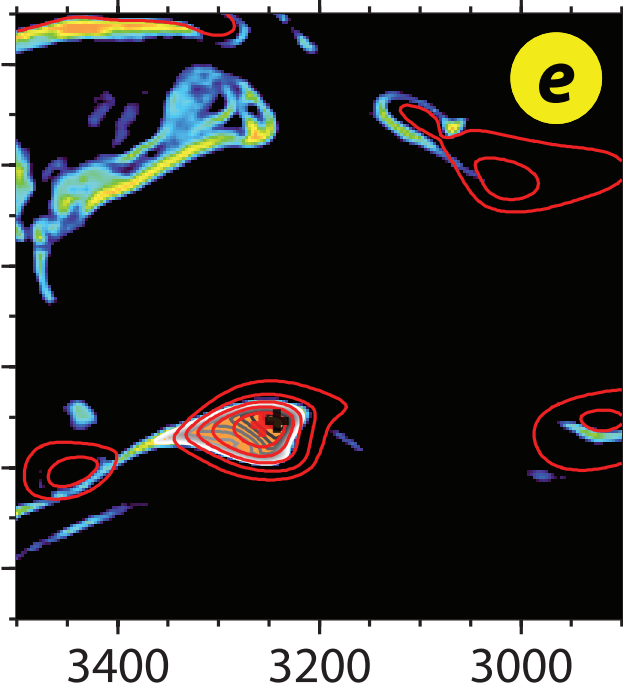
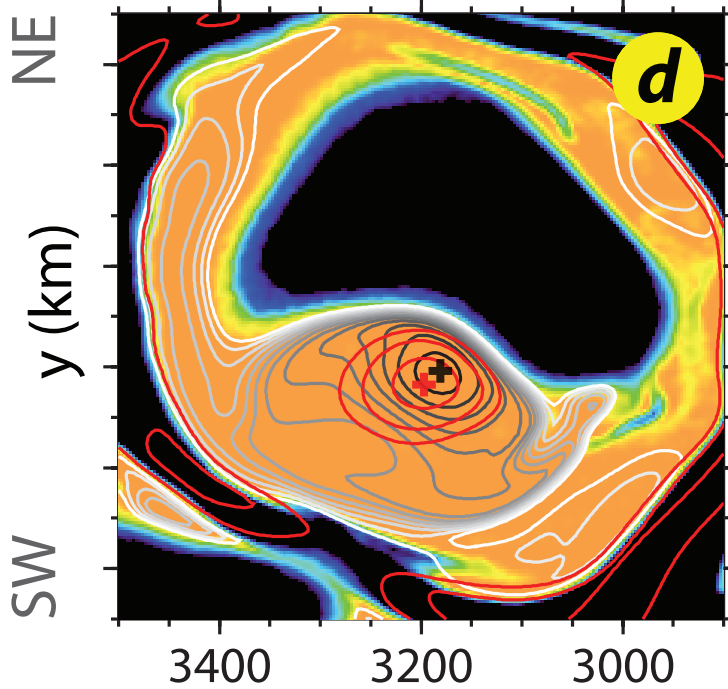
250 km

150 km



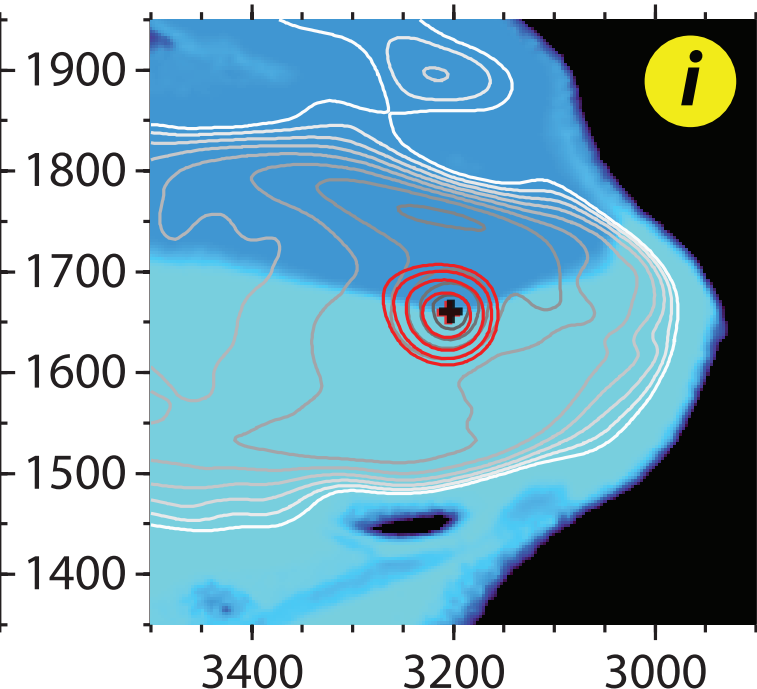
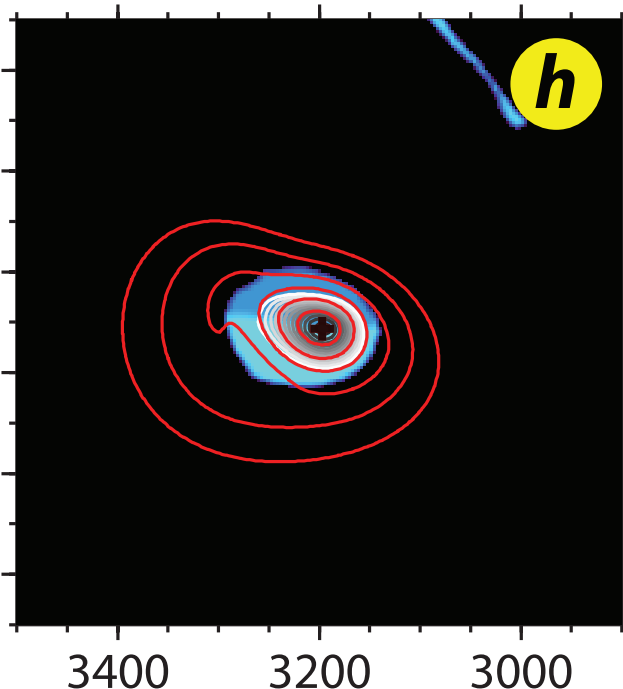
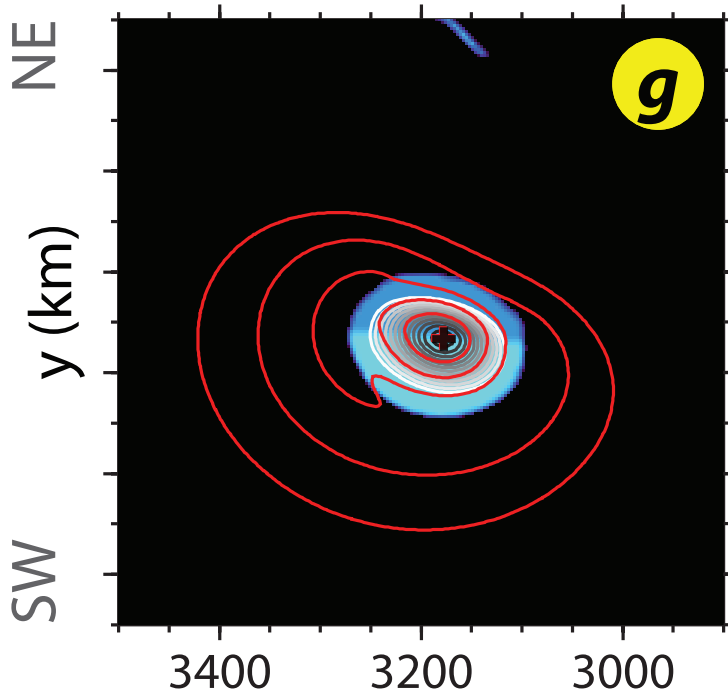
15%

case S1



15%

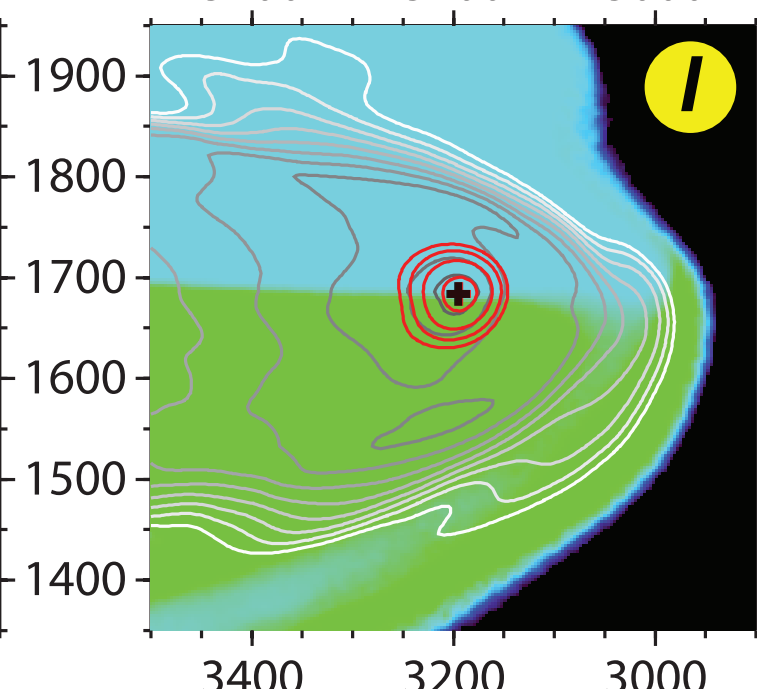
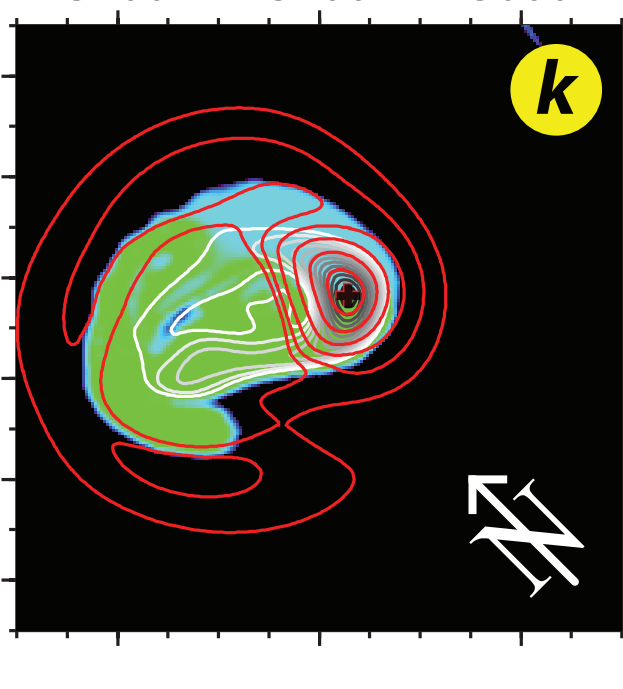
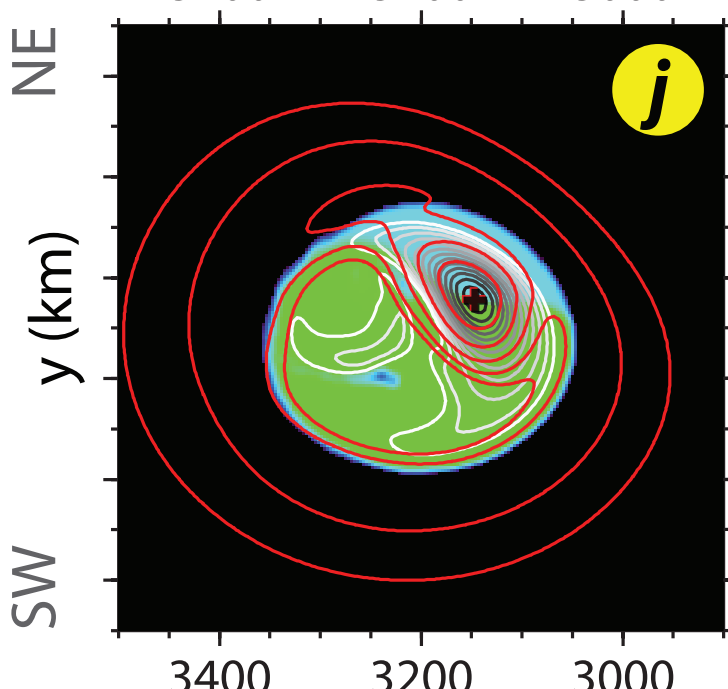
case S2



8%

10%

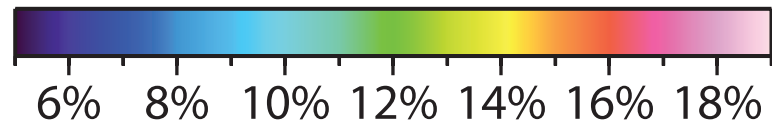
case Z1



10%

12%

case Z2



initial eclogite content

NW

SE

NW

SE

x (km)

x (km)

NE
y (km)
SW

NE
y (km)
SW

NE
y (km)
SW

NE
y (km)
SW

1900
1800
1700
1600
1500
1400

1900
1800
1700
1600
1500
1400

1900
1800
1700
1600
1500
1400

1900
1800
1700
1600
1500
1400

1900
1800
1700
1600
1500
1400

1900
1800
1700
1600
1500
1400

1900
1800
1700
1600
1500
1400

1900
1800
1700
1600
1500
1400

3400 3200 3000

3400 3200 3000

3400 3200 3000

3400 3200 3000

3400 3200 3000

3400 3200 3000

3400 3200 3000

3400 3200 3000

3400 3200 3000



