Collision of continental corner from 3-D numerical modeling

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A R T I C L E   I N F O

Article history:
Received 3 March 2013
Received in revised form 10 August 2013
Accepted 16 August 2013
Available online xxxx
Editor: C. Sotin

Keywords:
continental collision
lateral extrusion
slab break-off
3-D numerical modeling
Himalaya
Zagros

A B S T R A C T

Continental collision has been extensively investigated with 2-D numerical models assuming infinitely wide plates or insignificant along-strike deformation in the third dimension. However, the corners of natural collision zones normally have structural characteristics that differ from linear parts of mountain belts. We conducted 3-D high-resolution numerical simulations to study the dynamics of a continental corner (lateral continental/oceanic transition zone) during subduction/collision. The results demonstrate different modes between the oceanic subduction side (continuous subduction and retreating trench) and the continental collision side (slab break-off and topography uplift). Slab break-off occurs at a depth (≤100 km to ~300 km) that depends on the convergence velocity. The numerical models produce lateral extrusion of the overriding crust from the collisional side to the subduction side, which is also a phenomenon recognized around natural collision of continental corners, for instance around the western corner of the Arabia–Asia collision zone and around the eastern corner of the India–Asia collision zone. Modeling results also indicate that extrusion tectonics may be driven both from above by the topography and gravitational potentials and from below by the trench retreat and asthenospheric mantle return flow, which supports the link between deep mantle dynamics and shallower crustal deformation.

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1. Introduction

Continental subduction and collision normally follows oceanic subduction under the combined convergent forces of ‘ridge push’ and/or oceanic ‘slab pull’ (e.g., Turcotte and Schubert, 2002). Besides the systematic geological/petrological studies of recent continental collision zones (e.g., Alpine–Zagros–Himalayan belt), analogue (e.g., Chemenda et al., 1995, 1996, 2000; Boutelier et al., 2004) and numerical models (e.g., Beaumont et al., 2001, 2009; Burov et al., 2001; Liu et al., 2004; Toussaint et al., 2004; Burg and Gerya, 2005; Sobolev and Babeyko, 2005; Gerya et al., 2008a; Yamato et al., 2007, 2008; Warren et al., 2008; Li and Gerya, 2009; Li et al., 2010, 2011; Chen et al., 2013) are also widely used and become more and more substantial to investigate continental subduction/collision processes. The numerical tectonic styles of continental subduction/collision can be either “one-sided” (overriding plate does not subduct) or “two-sided” (both plates subduct together) (Tao and O’Connell, 1992; Pope and Willett, 1998; Facenda et al., 2008; Warren et al., 2008; Li et al., 2011). Several other possibilities such as thickening, slab drips (e.g., Toussaint et al., 2004) and slab break-off (e.g., Duretz et al., 2011, 2012; Van Hunen and Allen, 2011) have been put forward. The one-sided style can be further divided into steep (high angle) and flat (low angle) subduction/collision zones, resulting in different structures, stress states and deformation styles in the converging plates as well as different metamorphic pressure conditions of the exhumed wedge rocks (e.g., Li et al., 2011).

However, most of the models mentioned in the previous section are based on the 2-D regime, assuming that the plate is infinitely wide or that along-strike deformation in the third dimension can be neglected. 2-D models are indeed relevant to study the general processes and dynamics in the continental subduction channels and/or the interior of the continental collision zones, but far from curvilinear areas such as the continental corners. Recent 3-D numerical models of oceanic subduction, without continental collision, revealed different characteristics and scaling laws between the lateral edges and the interior of subducting slabs (e.g., Schellart et al., 2011; Li and Ribe, 2012). In nature, convergent continents have borders with transition to oceanic plates or to other continents. In addition, the corners of the natural collision zones normally have structures different from those of linear mountain belts. For example, the geological/petrological characteristics and deep structures of the western and eastern Himalayan syntaxes are very different from those of the central Himalayas (e.g., Burg et al., 1997; Burg and Podladchikov, 1999, 2000; Zeitler et al., 2001; Yin, 2006; Burg and Schmalholz, 2008; Guillot et al., 2008; Oreshin et al., 2008). Therefore, 3-D numerical
The evolution of the model (e.g., Figs. 2 and 3). Detailed properties of different rock processes are discussed.

The composition is either "air" (1 kg/m$^3$, above 12 km water level), or "water" (1000 kg/m$^3$, below y = -12 km water level), which has a low viscosity ($10^{19}$ Pas), Crameri et al. (2012) found that the sticky air approach is adequate as long as the term $(\eta_h/\eta_s)(h_{st}/L)^3$ is small, where $\eta_s$ and $\eta_h$ are the viscosity and thickness of the sticky air layer, and $h_{st}$ and $L$ are the characteristic viscosity and length scale of the model, respectively. According to this criterion, the quality of the internal free-surface condition in our models is rather moderate. But further decrease involving subduction of the lithospheric mantle. The Cartesian spatial domain is resolved by 501×341×165 grid points with the resolution of 2×2 km in the x-y plane and 4 km in the along-strike z-direction. The lithological structure of the model is represented by a dense grid of about 330 million randomly distributed markers used for advecting various material properties and temperatures.

The velocity boundary conditions are free slip at the top (y = 0) and at both the front and back boundaries (z = 0 and 656 km). The left and right boundaries (x = 0 and 1000 km) use constant normal velocities (convergence) in x-direction, which define the material influx through these side walls. For the permeable lower boundary condition (e.g., Burg and Gerya, 2005; Gerya et al., 2008a; Li et al., 2010), an external outflux boundary implies constant normal velocity and zero shear stress conditions to be satisfied at ~200 km below the base of the model domain. The external boundary condition allows global conservation of mass in the computational domain and is implemented by using the following limitation for velocity components at the lower boundary: $\partial V_y/\partial y = 0$, $\partial V_x/\partial y = 0$, $\partial V_y/\partial y = (V_{\text{external}} - V_y)/\Delta y_{\text{external}}$, where $\Delta y_{\text{external}}$ is the vertical distance from the lower boundary to the external boundary and $V_{\text{external}}$ is the constant normal velocity on the external boundary.

2.2. Material and thermal configuration

In the initial model setup, the overriding plate is homogeneous in the transverse z-direction. The subducting plate is composed of half continental (328 km wide) and half oceanic (328 km wide) lithospheres in z-direction (Fig. 1a), behind the oceanic-only subducting plate (656 km in z-direction and 500 km in x-direction). In the vertical section of the continental side (Fig. 1a and 1b) the initial material setup implies the 3-D transition from oceanic subduction to continental collision, which is similar to that of previous 2-D models (e.g., Gerya et al., 2008a; Li and Gerya, 2009; Li et al., 2011, 2012). In the continental domain, the initial material field incorporates a 35 km thick continental crust composed of 20 km upper crust and 15 km lower crust, resting on the 58 km lithospheric mantle and the subjacent 575 km asthenospheric mantle. The oceanic domain is comprised of an 8 km thick oceanic crust overlying the 82 km thick lithospheric mantle and the subjacent 575 km asthenospheric mantle. The viscous flow law of 'wet quartzite' describes the behavior of both the sediment and continental upper crust, while the 'Plagioclase An5%' represents the continental lower crust and the oceanic crust (Tables S2 and S3; Ranalli, 1995). Subduction initiation is imposed along a ~10 km thick weak zone dipping ~25° in the lithospheric mantle. This weak zone has a 'wet olivine' rheology in contrast to the 'dry olivine' rheology elsewhere in both the lithospheric and asthenospheric mantle. The rheological properties of hydrated and partially molten crustal and mantle rocks are shown in Tables S2 and S3.

The top surface of the lithosphere is calculated dynamically as an essentially internal free surface by using a buffer layer of 'sticky air' (Gerya and Yuen, 2003; Schmeling et al., 2008; Crameri et al., 2012). It is an initially 12–15 km thick layer above the upper crust, which changes dynamically during experiments. The composition is either "air" (1 kg/m$^3$, above y = -12 km water level) or "water" (1000 kg/m$^3$, below y = -12 km water level), which has a low viscosity ($10^{19}$ Pas), Crameri et al. (2012) found that the sticky air approach is adequate as long as the term $(\eta_h/\eta_s)(h_{st}/L)^3$ is small, where $\eta_s$ and $\eta_h$ are the viscosity and thickness of the sticky air layer, and $h_{st}$ and $L$ are the characteristic viscosity and length scale of the model, respectively. According to this criterion, the quality of the internal free-surface condition in our models is rather moderate. But further decrease
in the ‘sticky air’ viscosity and/or increase in its thickness are precluded by numerical limitations of the multigrid solver convergence. Indeed, the large viscosity contrast caused by this low-viscosity boundary layer minimizes shear stresses (~10^5 Pa) at the top of the solid portion of the model (Burg and Gerya, 2005). For simplicity, surface erosion and sedimentation are neglected, which is a first order approximation acceptable at the considered time and space scales.

The initial thermal structure of the subducting continental lithosphere (white lines in Fig. 1b) is laterally uniform with 0°C at the surface (<12 km, the air) and 1327°C at 100 km depth, with linear interpolation in between. The thermal structure of the overriding continental lithosphere is similar with 0°C at the surface, but 1322°C at 90 km depth (slightly warmer than the subducting continent). The relatively thin and hot continental lithosphere is applied in consistency with some mountain belts, such as Tibet (e.g., Owens and Zandt, 1997; Tilmann et al., 2003; Liang et al., 2012). The thermal structure of the oceanic lithosphere is applied using the half-space cooling age of 30 Ma (Turcotte and Schubert, 2002). The initial temperature gradient in the asthenospheric mantle is about 0.5°C/km. The thermal boundary conditions have a fixed value (0°C) for the upper boundary and zero horizontal heat flux across the vertical boundaries. For the lower thermal boundary, an infinity-like external constant temperature condition is imposed, which allows both temperatures and vertical heat fluxes to vary along the permeable lower boundary of the box. This implies that the constant temperature condition is satisfied at ~200 km below the bottom of the model. This condition is implemented by using the equation \( \frac{\partial T}{\partial y} = \left( T_{\text{external}} - T_y \right) / \Delta y_{\text{external}} \) at the lower boundary, where \( T_{\text{external}} \) is the temperature at the external boundary and \( \Delta y_{\text{external}} \) is the vertical distance from the lower boundary to the external boundary (e.g., Burg and Gerya, 2005; Gerya et al., 2008a; Li et al., 2010).

2.3. Hydration and melting implementation

In the numerical model, water is expelled from the subducted oceanic crust as a consequence of both dehydration reactions and compaction. Equilibrium mineralogical water content is calculated for the Lagrangian rock markers at every time step based on Gibbs free energy minimization (Connolly and Petrunj, 2002; Connolly, 2005: Gerya and Melilick, 2011) as a function of the local pressure, temperature and rock composition. The additional connate water content of the basaltic, upper oceanic crust and sediment is assumed as a linear function of depth.

\[
X_{H_2O(P)}(\text{wt.}%) = X_{H_2O(P_0)} \left( 1 - \Delta z / 75 \right)
\]

where \( X_{H_2O(P)} = 2 \text{ wt.} \% \) is the connate water content at the surface, \( \Delta z \) (km) is the depth below the surface in kilometer (0–75 km). The release of water also mimics the effects of low-temperature (T < 573 K) reactions not included in our thermodynamic database. According to the numerical models, water released from the slab creates a rheologically weak, hydrated zone, which ensures self-sustaining retreating subduction (Gerya et al., 2008b). To simulate the migration of water released by dehydration process, we use independently moving rock and fluid markers (Gorczyk et al., 2007a). To account for water transport, a fluid marker with its water amount is generated and moves upward until it reaches a lithology that assimilates water. Following Nikolaeva et al. (2008), the velocity of water is computed as

\[
\begin{align*}
V_x(\text{water}) &= V_x \\
V_y(\text{water}) &= V_y + V_{y(\text{percolation})} \\
V_z(\text{water}) &= V_z
\end{align*}
\]

where \( y \) is the vertical coordinate pointing upward, \( x \) and \( z \) are the horizontal coordinates, respectively; \( v_x, v_y \) and \( v_z \) indicate the local velocity, \( v_{y(\text{percolation})} = 10 \text{ cm/a} \), an assumed parameter (Peacock, 1990; Gorczyk et al., 2007b), characterizing the upward speed of free water through the mantle. The sensitivity tests of the percolation speed \( v_{y(\text{percolation})} \) on our results are shown in the supplementary Appendix (Figs. S1, S2). Free water is consumed by hydration and melting reactions in the mantle. Consequently, the propagation of the hydration/melting front in the mantle wedge is limited by the availability of water. This propagation is thus related to the rate of subduction which brings water to depths (Gerya et al., 2006).

The degree of melting of hydrated peridotite is computed as a function of pressure, temperature and water content using the parameterization of Katz et al. (2003). The degree of melting of crustal rocks is calculated according to the simple linear melting model (Burg and Gerya, 2005; Gerya and Melilick, 2011; Li et al., 2011):

\[
M = 0, \quad \text{when: } T \leq T_{\text{solidus}}
\]

\[
M = \left( T - T_{\text{solidus}} \right) / \left( T_{\text{liquidus}} - T_{\text{solidus}} \right), \quad \text{when: } T_{\text{solidus}} < T < T_{\text{liquidus}}
\]

\[
M = 1, \quad \text{when: } T \geq T_{\text{liquidus}}
\]

where \( M \) is the volumetric fraction of melt with temperature \( T \). \( T_{\text{solidus}} \) and \( T_{\text{liquidus}} \) are solids temperature and dry liquidus temperature at a given pressure and temperature, respectively (Table S3; Ranalli, 1995).

Consequently, the effective density, \( \rho_{\text{eff}} \), of partially molten rocks varies with the amount of melt fraction and \( P-T \) conditions according to the relations:

\[
\rho_{\text{eff}} = \rho_{\text{solid}} - M(\rho_{\text{solid}} - \rho_{\text{molten}})
\]

where \( \rho_{\text{solid}} \) and \( \rho_{\text{molten}} \) are the densities of the solid and molten crustal rock, respectively, which vary with pressure and temperature according to the relation:

\[
\rho_{P,T} = \rho_0 \left[ 1 - \alpha(T - T_0) \right] \left[ 1 + \beta(P - P_0) \right]
\]

where \( \rho_0 \) is the standard density at \( P_0 = 0.1 \text{ MPa} \) and \( T_0 = 298 \text{ K} \).

The effect of latent heating is implicitly included by increasing the effective heat capacity (\( C_{\text{p,eff}} \)) and thermal expansion (\( \alpha_{\text{eff}} \)) of partially molten rocks (0 < \( M < 1 \)), calculated as (Gerya, 2010):

\[
C_{\text{p,eff}} = C_p + Q_L \frac{\partial M}{\partial T} \bigg\rvert_{P=\text{const}}
\]

\[
\alpha_{\text{eff}} = \alpha + \frac{Q_L}{T} \frac{\partial M}{\partial P} \bigg\rvert_{T=\text{const}}
\]

where \( C_p \) and \( \alpha \) are the heat capacity and the thermal expansion of the solid crust, respectively, and \( Q_L \) is the latent heat of melting of the crust (Table S3).

2.4. Visco-plastic rheology

The relationships between the deviatoric stress (\( \sigma_{ij}' \)) and the strain rate (\( \dot{e}_{ij} \)) tensors are described by the visco-plastic constitutive laws allowing for strain localization (e.g., Buijter et al., 2006; Ruh et al., 2013). In case of incompressible viscous deformation, the viscous law of friction is:

\[
\begin{align*}
\sigma_{xx}' &= 2\eta_{\text{eff}} \dot{e}_{xx} \\
\sigma_{yy}' &= 2\eta_{\text{eff}} \dot{e}_{yy} \\
\sigma_{zz}' &= 2\eta_{\text{eff}} \dot{e}_{zz} \\
\sigma_{xy}' &= 2\eta_{\text{eff}} \dot{e}_{xy} \\
\sigma_{yz}' &= 2\eta_{\text{eff}} \dot{e}_{yz} \\
\sigma_{xz}' &= 2\eta_{\text{eff}} \dot{e}_{xz}
\end{align*}
\]

\[
\begin{align*}
\dot{e}_{xx} &= \frac{\partial \dot{v}_x}{\partial x} \\
\dot{e}_{yy} &= \frac{\partial \dot{v}_y}{\partial y} \\
\dot{e}_{zz} &= \frac{\partial \dot{v}_z}{\partial z}
\end{align*}
\]
\[ \dot{e}_{xy} = \frac{1}{2} \left( \frac{\partial v_x}{\partial y} + \frac{\partial v_y}{\partial x} \right) \]
\[ \dot{e}_{xz} = \frac{1}{2} \left( \frac{\partial v_x}{\partial z} + \frac{\partial v_z}{\partial x} \right) \]

(7)

where \( \eta_{\text{eff}} \) is the effective viscosity that depends on the pressure, temperature, composition, strain rate and degree of melting.

The viscosity for ductile creep is defined by:

\[ \eta_{\text{ductile}} = \left( \dot{\varepsilon}_H \right)^{1-n} \left( A_D \right)^{-1} \exp \left( -\frac{E + \rho V}{nRT} \right) \]

(8)

where \( \dot{\varepsilon}_H = (0.5k_{ij}k_{ij})^{1/2} \) is the second invariant of the strain rate tensor and \( A_D, E, V \) and \( n \) are experimentally determined flow law parameters (Tables S1 and S2), which stand for material constant, activation energy, activation volume and stress exponent, respectively.

The ductile rheology is combined with a brittle/plastic rheology to yield an effective visco-plastic rheology. The Drucker–Prager yield criterion, while in 2-D these two criteria are known to be equivalent. The Drucker–Prager yield criterion (e.g., Ranalli, 1995) was implemented as follows:

\[ \sigma_{\text{yield}} = C_0 + P \sin(\varphi_{\text{eff}}) \]
\[ \sin(\varphi_{\text{eff}}) = \sin(\varphi)(1 - \lambda) \]
\[ \eta_{\text{plastic}} = \frac{\sigma_{\text{yield}}}{2\dot{\varepsilon}_H} \]

(9)

where \( \sigma_{\text{yield}} \) is the yield stress, \( \dot{\varepsilon}_H \) is the second invariant of the strain rate tensor, \( P \) is the dynamic pressure; \( C_0 \) is the residual rock strength at \( P = 0 \) and \( \varphi \) is the internal frictional angle; \( \lambda \) is the pore fluid coefficient that controls the brittle strength of fluid-containing porous or fractured media. \( \varphi_{\text{eff}} \) can be illustrated as the effective internal frictional angle that integrates the effects of internal frictional angle \( \varphi \) and pore fluid coefficient \( \lambda \). In this paper, \( C_0 = 1 \text{ MPa} \) for all the rock types. Therefore the plastic rheology is implemented by different values of \( \sin(\varphi_{\text{eff}}) \) for different rock types (Table S3), which are chosen according to the same principles as in previous 2-D subduction/collision models (e.g., Gerya et al., 2008a; Li et al., 2011).

With \( \eta_{\text{ductile}} \) and \( \eta_{\text{plastic}} \), the visco-plastic rheology is assigned to the model by means of a Christmas tree-like criterion, where the rheological behavior depends on the minimum viscosity (or differential stress) attained between the ductile/plastic and brittle fields (Ranalli, 1995).

\[ \eta_{\text{creep}} = \min(\eta_{\text{ductile}}, \eta_{\text{plastic}}) \]

(10)

It is worth noting that elasticity might affect lithospheric flexure in collision zone, however, the general dynamics of continental subduction/collision and underlying mantle flow remain well established by the visco-plastic rheology (Gerya and Yuen, 2003, 2007).

2.5. Governing equations and numerical implementation

The momentum, continuity and heat conservation equations for a 3-D creeping flow are solved. Abbreviations and units are listed in Table S1.

(1) 3-D Stokes equations:

\[ \frac{\partial \sigma_{xx}'}{\partial x} + \frac{\partial \sigma_{xy}'}{\partial y} + \frac{\partial \sigma_{xz}'}{\partial z} = \frac{\partial P}{\partial x} \]
\[ \frac{\partial \sigma_{yx}'}{\partial x} + \frac{\partial \sigma_{yy}'}{\partial y} + \frac{\partial \sigma_{yz}'}{\partial z} = \frac{\partial P}{\partial y} - g \rho(C, M, P, T) \]
\[ \frac{\partial \sigma_{zx}'}{\partial x} + \frac{\partial \sigma_{zy}'}{\partial y} + \frac{\partial \sigma_{zz}'}{\partial z} = \frac{\partial P}{\partial z} \]

(11)

(2) Conservation of mass is approximated by the incompressible continuity equation:

\[ \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} + \frac{\partial v_z}{\partial z} = 0 \]

(12)

(3) Heat conservation equations:

\[ \rho C_p \left( \frac{DT}{Dt} \right) = \frac{\partial q_x}{\partial x} + \frac{\partial q_y}{\partial y} + \frac{\partial q_z}{\partial z} + H_r + H_a + H_S \]
\[ q_x = -k \frac{\partial T}{\partial x} \]
\[ q_y = -k \frac{\partial T}{\partial y} \]
\[ q_z = -k \frac{\partial T}{\partial z} \]
\[ H_a = T \alpha \frac{\partial P}{\partial x} \]
\[ H_S = \sigma_{xx} \dot{e}_{xx} + \sigma_{yy} \dot{e}_{yy} + \sigma_{zz} \dot{e}_{zz} + 2\sigma_{xy} \dot{e}_{xy} + 2\sigma_{xz} \dot{e}_{xz} \]

(13)

where \( y \) is the vertical coordinate pointing upward, \( x \) and \( z \) are the horizontal coordinates (Fig. 1); \( v_x, v_y, \) and \( v_z \) indicate the components of the velocity vector; \( t \) is time; \( \sigma_{ij} \) are the components of the viscous deviatoric stress tensor; \( \dot{\varepsilon}_{ij} \) are the components of the strain rate tensor; \( g \) is the gravitational acceleration, and the density \( \rho \) depends explicitly on composition (\( C \)), melt fraction (\( M \)), temperature (\( T \)) and pressure (\( P \)); \( k \) is the variable thermal conductivity (Clauser and Huenges, 1995). \( C_p \) is the effective isobaric heat capacity, i.e., incorporating latent heat; \( H_r, H_a \) and \( H_S \) denote radioactive heat production (Table S3), the energetic effect of isothermal (de)compression (i.e., adiabatic heating/cooling), and shear heating, respectively.

The above equations are solved in the ‘3ELVIS’ code (Gerya and Yuen, 2007; Zhu et al., 2009; Gerya, 2010) based on finite-differences with a marker-in-cell technique, which allows for non-diffusive numerical simulation of multiphase flow in a rectangular fully staggered Eulerian grid.

3. Model results

Series of numerical experiments were conducted with various convergence velocities \( V_c \). The partition of \( V_c \) is that \( V_c = V_{so} - V_{xs}, \) where \( V_{so} \) is applied on the boundary plane \( x = 0 \) km (overriding side), and \( V_{xs} \) on the boundary plane of \( x = 1000 \) km (subducting side: Fig. 1). In Models-I and -II, \( V_c = 5 \) cm/a (\( V_{so} = 1.5 \) cm/a, \( V_{xs} = -3.5 \) cm/a) for the first 10 Ma, which rules the oceanic subduction of 500 km. The partition of \( V_{so}/V_{xs} \) was determined in order to keep the subduction/collision zone in the middle of the model domain, far from the boundaries in \( x \)-direction. The ratio \( V_{so}/V_{xs} \) might affect the model evolution to a certain degree (Burov et al., in press). However, we emphasize that it does not change the general structures of the numerical models in a system with neglected inertia (Fig. S3). Then the convergence velocity was decreased linearly during continental subduction (10–15 Ma) to 2.5 cm/a for Model-I (Figs. 2a, 3a) and to 1 cm/a for Model-II (Fig. 6a). In Models-III and -IV, constant convergent velocities of 5 cm/a (\( V_{so} = 1.5 \) cm/a, \( V_{xs} = -3.5 \) cm/a; Fig. 7a) and 3.0 cm/a (\( V_{so} = 1 \) cm/a, \( V_{xs} = -2 \) cm/a; Fig. 8a) were applied, respectively. The configurations and detailed parameters are shown in Fig. 1 and Tables S2 and S3.

3.1. Reference Model-I

At the initial stages of our reference Model-I, the relatively strong oceanic plate subducted along the prescribed weak zone.
Fig. 2. Evolution of the reference model viewed in the oceanic subduction side. The top layer ($y > -20$ km) is cut off for clarity. The prescribed convergence velocity ($V_c$) decreases from 5 to 2.5 cm/a during the continental subduction (10–15 Ma) as shown in (a). The partition of $V_c$ is that $V_c = V_{xo} - V_{xs}$, where $V_{xo} = 1.5$ cm/a (in the initial model) is applied on the boundary plane $x = 0$ km (overriding side), and $V_{xs} = -3.5$ cm/a on the boundary plane of $x = 1000$ km (subducting side). The ratio $V_{xs}/V_{xo}$ is kept constant during the slowing of convergence. Colors of rock types are as in Fig. 1. Time (Ma) of shortening is given in the figures.

Fig. 3 also displays the topography evolution, which indicates that the relief of the continental collision mountain can reach 5–6 km in the overriding plate over a wide area (Figs. 3d–f).

Comparing Figs. 2 and 3 discloses the differences between the oceanic subduction and the continental collision sides. The $1000^\circ$C isotherm contour was plotted to make obvious the 3-D structure of the subducting slab (Fig. 4). On the oceanic side, subduction and trench retreat continue. By contrast, slab break-off occurs on the continental side in such a manner that the lateral integrity of the already subducted oceanic plate remains preserved (Fig. 4).
Fig. 3. Evolution of the reference model (same as Fig. 2) viewed in the continental collision side. The topography evolution is shown with the color scale in below.

Fig. 4. 3-D illustration of the subducting plate during slab break-off process, with the 1000 °C isotherm. The slab starts breaking near the lateral free-slip boundary on the continental collision side ($z = 656$ km), and the 'tear' is then propagating along-strike towards the continental edge (i.e., lateral continental/oceanic transition zone).

visualized (Fig. 5). They display how slab break-off evolves and the different styles of continental vs oceanic subduction. The surface velocity field demonstrates escape tectonics with material moving from the continental collision side to the oceanic subduction side (Figs. 5b, e). It also shows that extrusion velocity at the surface can be larger than the convergence velocity (Figs. 5b, e). The man-
Fig. 5. The effective viscosity ($\eta_{\text{eff}}$) and velocity ($v$) field at two stages: (a–c) 15.1 Ma, and (d–f) 21.4 Ma. (a, d) show $\eta_{\text{eff}}$ and $v$ for the whole model domain. (b, e) demonstrate the velocity field on a horizontal plane $y = -12$ km, which is the upper surface of the continent in the initial model, i.e. the boundary between the continent and the 'sticky air' (Fig. 1). (b′, e′) show the velocity field on a horizontal plane $y = -2$ km, for comparison. (c, f) plot a 3-D iso-viscosity contour ($\eta_{\text{eff}} = 10^{22}$ Pas). The arrows show the velocity field on a horizontal plane ($y = -240$ km), with the colors indicating the component of velocity in the $x$-direction $v_x$.

3.2. Model-II: slow continental collision

In Model-II, the prescribed convergence velocity ($V_c$) decreases from 5 to 1 cm/a during continental subduction (10–15 Ma, Fig. 6a). Therefore this model simulates larger convergence deceleration and slower collision rate than reference Model-I.

The general results of Model-II are similar to those of Model-I: (1) oceanic subduction and trench retreat are continuous with hydrated weak zone and partially molten rocks developed in the mantle wedge, closely above the subducting plate (Figs. 6a, b); (2) tearing of the slab after continental collision with exhumation of the subducted continental crust (Figs. 6c, d); and (3) lateral crustal extrusion from the collisional zone to the oceanic subduction side (Figs. 6b, d) along with mantle flux through the slab window from below the slab of the continental side towards the mantle wedge (Fig. 6f). However, since post-collision convergence is slow (1.0 cm/a after 15 Ma), the oceanic trench retreats relatively faster, opening a basin behind a rapidly retreating continental arc (Fig. 6b). Accordingly, the mantle flux through the slab window is faster than in Model-I (cf., Figs. 6f and 5f). Mantle flow further results in full decoupling between the subducting and the overriding plates (Fig. 6b). Break-off on the collision side occurs at shallower depth than in Model-I ($\leq 100$ km instead of ca 150 km; Figs. 6c and 3d). Crustal escape (i.e., lateral extrusion) in the overriding plate from the continental collision to the oceanic subduction side is faster, compensating the fast oceanic trench retreat (Figs. 6b, d). The high topography, which can reach about 5–6 km (Figs. 6c–d) during and after slab break-off, is localized near the collision zone. Significant back-arc extension and marginal-sea opening are worth noting in this model system (Fig. 6b).

3.3. Model-III: fast continental collision

In Model-III, the prescribed convergence velocity ($V_c$) keeps a constant value of 5 cm/a during the whole evolution from oceanic
Fig. 6. The model with prescribed convergence velocity ($V_c$) decreasing from 5 to 1 cm/a during the continental subduction (10–15 Ma) as shown in (a). The partition of $V_c$ is the same as in the reference model (Fig. 2), where $V_{so} = 1.5$ cm/a and $V_{sw} = -3.5$ cm/a at the beginning, and the $V_{sw}/V_{so}$ ratio is kept constant during the collision. (a–b) View in the oceanic subduction side. Colors of rock types are as in Fig. 1. (c–d) View in the continental collision side. The topography color scale is the same as in Fig. 2. (e–f) Iso-viscosity ($\eta = 10^{22}$ Pas) with the velocity field on a horizontal plane ($y = -240$ km). The velocity ($v_x$) color scale is the same as in Fig. 2. Time (Ma) of shortening is given in the figures.

subduction to continental collision (Fig. 7a). This model represents fast collision.

In Model-III, the position of the oceanic trench is rather stable (Figs. 7a, b). Consequently the mantle flux through the slab window is slower than in Models-I and -II (Figs. 7e, 5f and 6f). This produces coupling between the subducting oceanic plate and the overriding continental plate (Figs. 7a, b). The incoming continental plate subducts deeper than in Models-I and -II with slab tearing at about 250–300 km depth (Fig. 7c). After slab separation, the subducted part of the plate carrying continent up-bends as in the reference Model-I (Figs. 7d, 3f). In this fast convergent regime, the topography of the overriding continent is high over a wide area (Fig. 7d), in marked contrast to the localized high topography near the collision zone in the slow collision regime of Model-II (Fig. 6d).

3.4. Model-IV: slow oceanic subduction

Like Model-III, Model-IV was conducted with a constant but slower (3 cm/a) convergence velocity throughout the whole model evolution (Fig. 8a). This model was designed to investigate the influence of slow oceanic subduction.

The model yielded similar results as those from reference Model-I: (1) continuous subduction of the oceanic side with slow trench retreat; (2) slab torn apart on the continental collision side, at a depth of about 150 km, which leads to exhumation of continental crust; and (3) lateral material flow both in the deep asthenospheric mantle and in the shallower crust of the overriding plate. The main difference is that the subducted continental plate does not up-bend after break-off (Fig. 8d). Instead, the overriding plate tends to bend down and subduct also (so-called two-sided or ablative subduction; e.g., Faccenda et al., 2008; Li et al., 2011). This drag-down of the overriding plate is attributed to strong coupling between the subducting and overriding mantle lithospheres (Faccenda et al., 2008; Li et al., 2011).

4. Discussion

The subduction/collision of 3-D continental corners differs markedly from the general 2-D continental collision. In 2-D models, the material is confined in a vertical $x$–$y$ plane, without along-strike deformation (e.g., Li et al., 2011). In the current 3-D models, lateral extrusion occurs in the overriding crust from continental collision to the oceanic subduction side. The deeper mantle flow, after slab break-off, has also a large component in the along-strike $z$-direction. In addition, the 3-D numerical models provide significant insights on the combined oceanic subduction and continental collision. On the oceanic subduction side, the plate continues subducting and retreating with the trench retreat rate depending on the prescribed boundary convergence velocity (faster convergence, slower retreat). On the continental collision side, slab tearing and break-off occurs when the continental plate has subducted to a
Fig. 7. The model with constant convergence velocity \( (V_c = 5 \text{ cm/a}) \) as shown in (a). The partition of \( V_c \) is the same as in the reference model (Fig. 2), where \( V_m = 1.5 \text{ cm/a} \) and \( V_m = -3.5 \text{ cm/a} \). (a–b) View in the oceanic subduction side. Colors of rock types are as in Fig. 1. (c–d) View in the continental collision side. The topography color scale is the same as in Fig. 3. (e–f) Iso-viscosity \( (\eta = 10^{22} \text{ Pas}) \) with the velocity field on a horizontal plane \( (y = -240 \text{ km}) \). The velocity \( (v_x) \) color scale is the same as in Fig. 5. Time (Ma) of shortening is given in the figures.

The following discussion is organized around the principal aims of this study, which are (1) 3-D slab break-off dynamics, (2) lateral extrusion mechanism, and (3) implications for the eastern Alpine–Himalayan belt.

4.1. Three-dimensional slab break-off

The concept of slab tearing and break-off comes from interpretations of geophysical/geochemical observations in the subduction/collision zones, e.g., the positive seismic velocity anomalies interpreted as detached slab segments under India and the Himalayas (Van der Voo et al., 1999) and in the Mediterranean region (Wortel and Spakman, 2000). As summarized in Duretz et al. (2012), slab break-off has two major consequences: (1) partial or complete loss of the slab pull force and (2) inflow of hot asthenosphere where the slab ruptured. The first consequence is commonly used to explain tectonic processes such as surface uplift (Rogers et al., 2002), orogenic extension (Zeck, 1996) and exhumation of high pressure rocks (Andersen et al., 1991; Xu et al., 2010). The second consequence is usually considered to be an efficient mechanism for advecting heat at lithospheric to sub-crustal level, which triggers partial melting and plutonism (e.g., Davies and von Blanckenburg, 1995; Ferrari, 2004; Liu and Stegman, 2012).

Slab break-off has already been investigated by several analytical (e.g., Schmalholz, 2011), analogue (e.g., Regard et al., 2008) and numerical models (e.g., Davies and von Blanckenburg, 1995; Ton and Wortel, 1997; Buiter et al., 2002; Gerya et al., 2004; Toussaint et al., 2004; Burkett and Billen, 2010; Van Hunen and Allen, 2011; Duretz et al., 2011, 2012). 2-D numerical simulations (Duretz et al., 2011) demonstrate variable end-members, i.e. shallow (~40 km depth), intermediate (~200 km) and deep (~300 km) slab break-off. In our numerical models, the relationship between depth of slab break-off \( (D) \) and convergence velocity during continental collision \( (V_c) \) is: (1) shallow break-off \( (D \leq 100 \text{ km}) \); Fig. 6c, \( V_c = 1 \text{ cm/a} \), (2) intermediate break-off \( (D \sim 150 \text{ km}) \); Figs. 3d, 8c, \( V_c = 2.5-3 \text{ cm/a} \), and (3) deep break-off \( (D = 250-300 \text{ km}) \); Fig. 7c, \( V_c = 5 \text{ cm/a} \). These results are consistent with 2-D simulations (Duretz et al., 2011), but the convergence rate in our 3-D models is applied by both ‘ridge push’ and ‘slab pull’, while it is only ‘slab pull’ in the referenced 2-D models. Recent 3-D models (Van Hunen and Allen, 2011) have shown that break-off propagates parallel to the trench, which can be either from somewhere within the slab to its edges in a symmetric collision setting, or from one edge to within the slab in an asymmetric setting. The dominant deformation mechanism during break-off is considered to be viscous necking (e.g., Schmalholz, 2011; Van Hunen and Allen, 2011; Duretz et al., 2012).

In our 3-D models, slab break-off is initiated away from the continental corner, at the free-slip model boundary (e.g., Fig. 4b), which actually would be within the continental plate. The 3-D...
Fig. 8. The model with constant convergence velocity \( V_c = 3 \text{ cm/a} \) as shown in (a), where \( V_{so} = 1 \text{ cm/a} \) and \( V_{so} = -2 \text{ cm/a} \). (a–b) View in the oceanic subduction side. Colors of rock types are as in Fig. 1. (c–d) View in the continental collision side. The topography color scale is the same as in Fig. 3. (e–f) Iso-viscosity \( (\eta_{\text{eff}} = 10^{22} \text{ Pas}) \) with the velocity field on a horizontal plane \( (y = -240 \text{ km}) \). The velocity \( (v_x) \) color scale is the same as in Fig. 5. Time (Ma) of shortening is given in the figures.

style of slab break-off agrees with the results of Van Hunen and Allen (2011), but the trench-parallel tear propagation is limited by the cornered ocean-continent boundary. There, the tear does not propagate into the oceanic slab. Instead, it turns along the lateral continent boundary. In this system, the integrated slab pull is transmitted into the retreating oceanic subduction domain.

Our 3-D numerical simulations indicate that slab break-off plays fundamental roles in the dynamics of continental (corner) collision: (1) up-bending of the subducted continental plate after loss of slab pull along the former ocean-continent boundary (Figs. 3f, 7d), which does not appear in Model-IV (Fig. 8d) because of the tendency of two-sided subduction under coupled, high stress regime; (2) topography uplift in the collision zone (Fig. 3); and (3) asthenospheric mantle flow through the tear window (Fig. 5).

4.2. Lateral extrusion mechanism

Lateral extrusion was obtained in all models (Figs. 2, 6, 7 and 8), which suggests that escape tectonics is a common feature to all colliding continental corners. Comparing the models, lateral extrusion appears to depend on three factors:

1. Continental collision and topography build-up; there is no lateral extrusion before onset of continental collision (Figs. 2a, 2b, 3a, 3b). Collision produces the necessary topography and gravitational potential, which can be regarded as a 'source' for material extrusion (e.g., Royden et al., 2008).

2. Positive correlation with the trench retreat rate; faster trench retreat results in faster lateral extrusion (Fig. 6b). Conversely, slower trench retreat leads to slower extrusion (Fig. 7b). The intermediate trench retreat rate produces intermediate lateral material extrusion (Figs. 2f, 8b). Trench retreat causes extension in the upper plate, which provides a 'sink' region to receive the extruded materials.

3. Slab break-off and mantle flow through the slab window (e.g., Fig. 5), which together facilitate trench retreat, hence lateral extrusion. Lateral extrusion expresses the link between deep mantle dynamics and crustal processes.

It is worth noting that surface processes, i.e. erosion and sedimentation, may influence the lateral extrusion to a certain degree. However their rates and scales are too small to change the general structure and dynamics of the continental collision (e.g., Li and Gerya, 2009). For the sake of simplicity, they were both neglected in the present models.

4.3. Implications for the eastern Alpine–Himalayan belt

The Alpine–Himalayan belt is one of the youngest and best documented continental convergent zones, which formed after closure of the Tethys Ocean. The eastern part of this convergent belt (Fig. 9) is composed of two continental collision zones alternating with three oceanic subduction zones (e.g., Vernant et al., 2004; Hatzfeld and Molnar, 2010; Yin, 2010): (1) the oceanic subduction
zone in the eastern Mediterranean Sea (MS), with the overriding Anatolian (western Turkey) plate being extruded westward; (2) the Arabia–Asia collision zone that produced the Zagros fold-thrust belt; (3) the Arabian Sea subduction under the Makran Accretionary Complex; (4) the South-Tibet–Himalaya thrust belt due to the India–Asia collision; and (5) the Indonesian oceanic subduction in the Bay of Bengal and Indian Ocean, with the east–southeastward extrusion of Asian blocks in the overriding plate. This orogenic system involves four continental corners, two symmetrical ones in front of Arabia, and two equally symmetrical in front of India. Due to computational limitations, we simulated collision of only one continental corner neighboring a piece of oceanic subduction zone, assuming that essential results can be applied to all natural cases through simple symmetry.

In the eastern Alpine–Himalayan belt, GPS data document lateral extrusion of Anatolia around the western corner of the Arabia–Asia collision zone (e.g., McClusky et al., 2000; Sengor et al., 2005; Reilinger et al., 2010), as well as escape of southeast Asia around the eastern corner of the India–Asia collision zone (e.g., Wang et al., 2001; Zhang et al., 2004). A dextral strike-slip fault system (Dehshir Fault, Kuh Banan Fault, Nayband Fault, Fig. 9) delineates the eastern side of the Arabia–Asia collision zone, accommodating northward penetration of Arabia into Asia. The sinistral Chaman fault system delimits the west-side of the India–Asia collision zone (Fig. 9), accommodating northward penetration of India into Asia. This pattern permits a relative southward extrusion of Iranian Blocks and the Makran Accretionary Complex between the two collision zones, but the GPS velocities are scarce over most parts of this region (e.g., Vernant et al., 2004; Hatzfeld and Molnar, 2010). Weaker extrusion of this eastern side compared to extrusion of Anatolia, in the west, may reflect narrow oceanic basins, thus limited subduction between the two collision belts (Fig. 9).

Extrusion of Anatolia is generally attributed to the Arabia–Asia collision as well as the southwestern retreat of the eastern Mediterranean subduction trench (e.g., Le Pichon and Angelier, 1979; Lister et al., 1984; Sengor et al., 2005; Ring et al., 2001; Hubert-Ferrari et al., 2002; Westaway, 2004; Marsellos and Kidd, 2008; Yin, 2010). On the one hand, trench retreat and the induced ‘Aegean’ extension could have facilitated lateral extrusion of Anatolia. On the other hand, northward penetration of the Arabian plate into Asia may have pushed the asthenosphere beneath Zagros in a counterclockwise flow pattern (e.g., Yin, 2010), which forced the eastern Mediterranean slab to retreat. Jolivet et al. (2013) also suggest that extrusion of Anatolia is partly driven from below by the trench retreat induced asthenospheric flow (in agreement with the SKS fast directions) and partly from above by the extrusion of a lid of rigid crust (consistent with the stretching lineations in the crust). This association indicates connections between continental collision, oceanic trench retreat and lateral extrusion, as in our numerical models.

The extrusion of southeast Asia results from the ca 50 Ma old India–Asia collision (e.g., Tapponnier et al., 1982, 1986, 2001), which could either be the cause of marginal-sea opening such as the South China Sea (Fig. 9; e.g., Tapponnier et al., 1982; Peltzer and Tapponnier, 1988) or a result of trench retreat (e.g., Royden et al., 2008). Eastward lithospheric extrusion from central Tibet took place during a time of rapid trench rollback along much of the Pacific, Philippine, and Indonesian oceanic subduction boundaries (e.g., Tapponnier et al., 1986; van der Hilst and Seno, 1993). The Pacific and Philippine subduction, to the east of the southeast Asia extrusion system, is not included in either Fig. 9 or the numerical simulations. By contrast, the Indonesian subduction zone (Fig. 9) is treated as the oceanic subduction side in the numerical models (e.g., Fig. 2), which thereby plays a similar role as the eastern Mediterranean trench in the Anatolian extrusion system.

The scale of lateral extrusion around the corner of continent in the numerical models is about 200–300 km (Figs. 2, 5), which is smaller than the natural Anatolia and southeast Asia extrusion zones. The smallness of experimental extrusion is mainly attributed to the relatively small width of the models (656 km in z-direction) limited to that size because of the heavy computation in 3-D high-resolution numerical simulations. The model domain is laterally bounded by two free-slip vertical planes (z = 0 and 656 km), on which the normal velocity and shear stresses are zero. Therefore, material extrusion around the continental corner can only have a relatively small width, rather than moving laterally far away from the collision front. Although the computational limitation prevents reproducing the large size of laterally escaped blocks, the numerical models reveal similar geodynamical processes and provide significant insights into the mechanism of lateral extrusion tectonics. In addition, laterally heterogeneous structures (crustal thickness, thermal state, rheological structure, lithology, etc.) of different continental blocks may also play a major role in organization of 3-D patterns of plate tectonics in the eastern Alpine–Himalayan belt (Fig. 9). However numerical simulation of these factors is still prevented by the current computational limitations.
5. Conclusions

3-D numerical models of continental collision limited by a corner boundary with adjacent oceanic lithosphere simulated different, yet linked and coeval tectonic styles. The oceanic plate keeps subducting with trench retreat, without break-off. On the continental side, slab tearing and break-off occurs at a depth (≤100 km to ~300 km) related to the convergence velocity (faster convergence, larger depth). The slab tear window is first initiated away from the continental corner, then propagates along-strike to the edge of the continental plate, and finally, at a shallower depth, along the lateral continental/oceanic transition zone. The structures and dynamics of slab break-off are consistent with and further develop the previous 2-D and 3-D models (e.g., Duret et al., 2011; Van Hunen and Allen, 2011). Numerical experiments also simulate lateral extrusion tectonics and establish that it should be a general phenomenon during collision of continental corners. Lateral extrusion is driven both from above by the topography and gravitational potentials and from below by the trench retreat and asthenospheric mantle return flow.

Acknowledgements

This work was supported by the Start-up Research Fund from Institute of Geology of CAGS (J1219) and the fund from NSFC (40921001), China Geological Survey projects (1212011121275, 1212011120161), and Sinoprobe project to ZHL. TG is supported by ETH Research Grants ETH-0807-3, ETH-0609-2 and TopoEurope program. G. Zhu, D. May and T. Duret are thanked for the discussion of 3-D visualization. We also thank M. Liu for fruitful discussion and reviews of the geological papers. Thorough and constructive reviews by C. Beaumont and two anonymous reviewers are much appreciated.

Appendix A. Supplementary material

Supplementary material related to this article can be found online at http://dx.doi.org/10.1016/j.epsl.2013.08.034.

References


